

Building Optimization-Enabled Applications Using AMPL API

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Optimization Modeling and Beyond with a Focus on Practice

Building Optimization-Enabled Applications Using AMPL API

We describe how to combine the power of the AMPL modeling system and a general-purpose programming language to build rich optimization-enabled client applications. Having an optimization model expressed in a high-level declarative form with model and data separation facilitates its evolution and maintenance, and makes switching between different solvers and data sources easy. At the same time it is possible to use a familiar development environment and have access to a wide variety of programming libraries for data management and interface development.



Features

- ❖ Algebraic modeling language
- ❖ Built specially for optimization
- ❖ Designed to support many solvers

Design goals

- ❖ Powerful, general expressions
- ❖ Natural, easy-to-learn modeling principles
- ❖ Efficient processing that scales well with problem size

3 ways to use . . .

3 Ways to Use AMPL

Command language

- ❖ Browse results & debug model interactively
- ❖ Make changes and re-run

Scripting language

- ❖ Bring the programmer to the modeling language

Programming interface (API)

- ❖ Bring the modeling language to the programmer

Example

Roll cutting model

- ❖ Solution via command language
- ❖ Tradeoff analysis via scripting

Roll cutting by pattern enumeration

- ❖ via scripting
- ❖ via API

Roll cutting by pattern generation

- ❖ via scripting
- ❖ via API

Roll Cutting Problem

Motivation

- ❖ Fill orders for rolls of various widths
 - * by cutting raw rolls of one (large) fixed width
 - * using a variety of cutting patterns

Optimization model

- ❖ Decision variables
 - * number of raw rolls to cut according to each pattern
- ❖ Objective
 - * minimize number of raw rolls used
- ❖ Constraints
 - * meet demands for each ordered width

Roll cutting

Mathematical Formulation

Given

W set of ordered widths

n number of patterns considered

and

a_{ij} occurrences of width i in pattern j ,
for each $i \in W$ and $j = 1, \dots, n$

b_i orders for width i , for each $i \in W$

Roll cutting

Mathematical Formulation (*cont'd*)

Determine

X_j number of rolls to cut using pattern j ,
for each $j = 1, \dots, n$

to minimize

$$\sum_{j=1}^n X_j$$

total number of rolls cut

subject to

$$\sum_{j=1}^n a_{ij} X_j \geq b_i, \text{ for all } i \in W$$

number of rolls of width i cut
must be at least the number ordered

Roll Cutting

AMPL Formulation

Symbolic model

```
set WIDTHS;  
param orders {WIDTHS} > 0;  
param nPAT integer >= 0;  
param nbr {WIDTHS,1..nPAT} integer >= 0;  
  
var Cut {1..nPAT} integer >= 0;  
  
minimize Number:  
    sum {j in 1..nPAT} Cut[j];  
  
subj to Fulfill {i in WIDTHS}:  
    sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

$$\sum_{j=1}^n a_{ij} X_j \geq b_i$$

Roll Cutting

AMPL Formulation (*cont'd*)

Explicit data (independent of model)

```
param: WIDTHS: orders :=
    6.77    10
    7.56    40
    17.46   33
    18.76   10 ;

param nPAT := 9 ;

param nbr:  1  2  3  4  5  6  7  8  9 :=
    6.77    0  1  1  0  3  2  0  1  4
    7.56    1  0  2  1  1  4  6  5  2
    17.46   0  1  0  2  1  0  1  1  1
    18.76   3  2  2  1  1  1  0  0  0 ;
```

Command Language

Model + data = problem instance to be solved

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver cplex;
ampl: solve;
CPLEX 12.6.3.0: optimal integer solution; objective 20
3 MIP simplex iterations
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13 7 4 9 3
```

Command Language (*cont'd*)

Solver choice independent of model and data

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver gurobi;
ampl: solve;
Gurobi 7.0.0: optimal solution; objective 20
3 simplex iterations
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13  7 4  9 3
```

Command Language (*cont'd*)

Results available for browsing

```
ampl: display {j in 1..nPAT, i in WIDTHS: Cut[j] > 0} nbr[i,j];
:      4   7   9   :=                                # patterns used
6.77   0   0   4
7.56   1   6   2
17.46  2   1   1
18.76  1   0   0

ampl: display {j in 1..nPAT} sum {i in WIDTHS} i * nbr[i,j];
1 63.84   3 59.41   5 64.09   7 62.82   9 59.66      # pattern
2 61.75   4 61.24   6 62.54   8 62.0          # total widths

ampl: display Fulfill.slack;
6.77  2                                # overruns
7.56  3
17.46 0
18.76 3
```

Roll Cutting

Revision 1: Waste vs. # of Rolls

Symbolic model

```
param roll_width > 0;

set WIDTHS;
param orders {WIDTHS} > 0;

param nPAT integer >= 0;
param nbr {WIDTHS,1..nPAT} integer >= 0;

var Cut {1..nPAT} integer >= 0;

minimize Number:
    sum {j in 1..nPAT} Cut[j];

minimize Waste:
    sum {j in 1..nPAT}
        Cut[j] * (roll_width - sum {i in WIDTHS} i * nbr[i,j]);

subj to Fulfill {i in WIDTHS}:
    sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

Roll Cutting

Revision 1 (*cont'd*)

Explicit data

```
param roll_width := 64.5;

param: WIDTHS: orders :=
    6.77    10
    7.56    40
    17.46   33
    18.76   10 ;

param nPAT := 9 ;

param nbr: 1 2 3 4 5 6 7 8 9 :=
    6.77  0 1 1 0 3 2 0 1 4
    7.56  1 0 2 1 1 4 6 5 2
    17.46 0 1 0 2 1 0 1 1 1
    18.76 3 2 2 1 1 1 0 0 0 ;
```

Revision 1 (*cont'd*)

Solutions

```
ampl: model cutRev1.mod;
ampl: data cutRev1.dat;

ampl: objective Number; solve;
Gurobi 7.0.0: optimal solution; objective 20
3 simplex iterations
ampl: display Number, Waste;
Number = 20
Waste = 63.62

ampl: objective Waste; solve;
Gurobi 7.0.0: optimal solution; objective 15.62
2 simplex iterations
ampl: display Number, Waste;
Number = 35
Waste = 15.62
```


Roll Cutting

Revision 2: Overrun Limit

Symbolic model

```
param roll_width > 0;
param over_lim integer >= 0;

set WIDTHS;
param orders {WIDTHS} > 0;

param nPAT integer >= 0;
param nbr {WIDTHS,1..nPAT} integer >= 0;

var Cut {1..nPAT} integer >= 0;

...

subj to Fulfill {i in WIDTHS}:
    orders[i] <= sum {j in 1..nPAT} nbr[i,j] * Cut[j]
    <= orders[i] + over_lim;
```

Roll Cutting

Revision 2 (cont'd)

Explicit data

```
param roll_width := 64.5;
param over_lim := 6 ;

param: WIDTHS: orders :=
    6.77    10
    7.56    40
    17.46   33
    18.76   10 ;

param nPAT := 9 ;

param nbr:  1  2  3  4  5  6  7  8  9 :=
    6.77  0  1  1  0  3  2  0  1  4
    7.56  1  0  2  1  1  4  6  5  2
    17.46 0  1  0  2  1  0  1  1  1
    18.76 3  2  2  1  1  1  0  0  0 ;
```

Revision 2 (*cont'd*)

Solutions

```
ampl: model cutRev2.mod;
ampl: data cutRev2.dat;

ampl: objective Number; solve;
Gurobi 7.0.0: optimal solution; objective 20
7 simplex iterations
ampl: display Number, Waste;
Number = 20
Waste = 54.76

ampl: objective Waste; solve;
Gurobi 7.0.0: optimal solution; objective 49.16
4 simplex iterations
ampl: display Number, Waste;
Number = 21
Waste = 49.16
```

Scripting

Bring the programmer to the modeling language

Extend modeling language syntax . . .

- ❖ Algebraic expressions
- ❖ Set indexing expressions
- ❖ Interactive commands

. . . with programming concepts

- ❖ Loops of various kinds
- ❖ If-then and If-then-else conditionals
- ❖ Assignments

Examples

- ❖ Tradeoffs between objectives
- ❖ Cutting *via* pattern enumeration
- ❖ Cutting *via* pattern generation

Scripting

Tradeoffs Between Objectives

Minimize rolls cut

- ❖ Set large overrun limit

Minimize waste

- ❖ Reduce overrun limit 1 roll at a time
- ❖ If there is a change in number of rolls cut
 - * record total waste (increasing)
 - * record total rolls cut (decreasing)
- ❖ Stop when no further progress possible
 - * problem becomes infeasible
 - * total rolls cut falls to the minimum
- ❖ Report table of results

Scripting

Parametric Analysis (*cont'd*)

Script (setup and initial solve)

```
model cutRev2.mod;
data cutRev2.dat;

set OVER default {} ordered by reversed Integers;

param minNumber;
param minNumWaste;
param minWaste {OVER};
param minWasteNum {OVER};

param prev_number default Infinity;

option solver gurobi;
option solver_msg 0;

objective Number;
solve >Nul;

let minNumber := Number;
let minNumWaste := Waste;

objective Waste;
```

Scripting

Parametric Analysis (*cont'd*)

Script (looping and reporting)

```
for {k in over_lim .. 0 by -1} {
  let over_lim := k;
  solve >Nul;
  if solve_result = 'infeasible' then break;
  if Number < prev_number then {
    let OVER := OVER union {k};
    let minWaste[k] := Waste;
    let minWasteNum[k] := Number;
    let prev_number := Number;
  }
  if Number = minNumber then break;
}

printf 'Min%3d rolls with waste%6.2f\n\n', minNumber, minNumWaste;
printf ' Over Waste Number\n';
printf {k in OVER}: '%4d%8.2f%6d\n', k, minWaste[k], minWasteNum[k];
```

Scripting

Parametric Analysis (*cont'd*)

Script run

```
AMPL: include cutWASTE.run
```

```
Min 20 rolls with waste 62.04
```

Over	Waste	Number
10	46.72	22
7	47.89	21
5	54.76	20

```
AMPL:
```


Scripting

Cutting *via* Pattern Enumeration

Build the pattern list, then solve

- ❖ Read general model
- ❖ Read data: demands, raw width
- ❖ Compute data: all usable patterns
- ❖ Solve problem instance

Scripting

Pattern Enumeration

Model

```
param roll_width > 0;
set WIDTHS ordered by reversed Reals;
param orders {WIDTHS} > 0;

param maxPAT integer >= 0;
param nPAT integer >= 0, <= maxPAT;

param nbr {WIDTHS,1..maxPAT} integer >= 0;

var Cut {1..nPAT} integer >= 0;

minimize Number:
    sum {j in 1..nPAT} Cut[j];

subj to Fulfill {i in WIDTHS}:
    sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

Scripting

Pattern Enumeration

Data

```
param roll_width := 64.50 ;  
param: WIDTHS: orders :=  
    6.77    10  
    7.56    40  
    17.46   33  
    18.76   10 ;
```

Scripting

Pattern Enumeration

Script (initialize)

```
model cutPAT.mod;
data Sorrentino.dat;

param curr_sum >= 0;
param curr_width > 0;
param pattern {WIDTHS} integer >= 0;

let maxPAT := 1000000;

let nPAT := 0;
let curr_sum := 0;
let curr_width := first(WIDTHS);
let {w in WIDTHS} pattern[w] := 0;
```

Scripting

Pattern Enumeration

Script (loop)

```
repeat {
  if curr_sum + curr_width <= roll_width then {
    let pattern[curr_width] := floor((roll_width-curr_sum)/curr_width);
    let curr_sum := curr_sum + pattern[curr_width] * curr_width;
  }
  if curr_width != last(WIDTHS) then
    let curr_width := next(curr_width,WIDTHS);
else {
  let nPAT := nPAT + 1;
  let {w in WIDTHS} nbr[w,nPAT] := pattern[w];
  let curr_sum := curr_sum - pattern[last(WIDTHS)] * last(WIDTHS);
  let pattern[last(WIDTHS)] := 0;
  let curr_width := min {w in WIDTHS: pattern[w] > 0} w;
  if curr_width < Infinity then {
    let curr_sum := curr_sum - curr_width;
    let pattern[curr_width] := pattern[curr_width] - 1;
    let curr_width := next(curr_width,WIDTHS);
  }
  else break;
}
}
```

Scripting

Pattern Enumeration

Script (solve, report)

```
option solver gurobi;
solve;
printf "\n%5i patterns, %3i rolls", nPAT, sum {j in 1..nPAT} Cut[j];
printf "\n\n Cut  ";
printf {j in 1..nPAT: Cut[j] > 0}: "%3i", Cut[j];
printf "\n\n";
for {i in WIDTHS} {
    printf "%7.2f ", i;
    printf {j in 1..nPAT: Cut[j] > 0}: "%3i", nbr[i,j];
    printf "\n";
}
printf "\nWASTE = %5.2f%\n\n",
    100 * (1 - (sum {i in WIDTHS} i * orders[i]) / (roll_width * Number));
```

Scripting

Pattern Enumeration

Results

```
ampl: include cutPatEnum.run
```

```
Gurobi 7.0.0: optimal solution; objective 18
```

```
5 simplex iterations
```

43 patterns, 18 rolls

```
Cut      2  2  3 11
```

```
18.76   3  2  0  0
```

```
17.46   0  1  3  2
```

```
7.56    1  1  1  3
```

```
6.77    0  0  0  1
```

```
WASTE = 2.34%
```

Scripting

Cutting via Pattern Generation

Generate the pattern list by a series of solves

- ❖ Solve LP relaxation using subset of patterns
- ❖ Add “most promising” pattern to the subset
 - * Minimize reduced cost given dual values
 - * Equivalent to a knapsack problem
- ❖ Iterate as long as there are promising patterns
 - * Stop when minimum reduced cost is zero
- ❖ Solve IP using all patterns found

Scripting

Pattern Generation

Cutting model

```
set WIDTHS ordered by reversed Reals;
param orders {WIDTHS} > 0;

param nPAT integer >= 0, <= maxPAT;
param nbr {WIDTHS,1..nPAT} integer >= 0;

var Cut {1..nPAT} integer >= 0;

minimize Number:
    sum {j in 1..nPAT} Cut[j];

subj to Fulfill {i in WIDTHS}:
    sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

Scripting

Pattern Generation

Knapsack model

```
param roll_width > 0;
param price {WIDTHS} default 0.0;

var Use {WIDTHS} integer >= 0;

minimize Reduced_Cost:
    1 - sum {i in WIDTHS} price[i] * Use[i];

subj to Width_Limit:
    sum {i in WIDTHS} i * Use[i] <= roll_width;
```

Scripting

Pattern Generation

Script (problems, initial patterns)

```
model cutPatGen.mod;
data Sorrentino.dat;

problem Cutting_Opt: Cut, Number, Fill;
    option relax_integrality 1;
    option presolve 0;

problem Pattern_Gen: Use, Reduced_Cost, Width_Limit;
    option relax_integrality 0;
    option presolve 1;

let nPAT := 0;
for {i in WIDTHS} {
    let nPAT := nPAT + 1;
    let nbr[i,nPAT] := floor (roll_width/i);
    let {i2 in WIDTHS: i2 <> i} nbr[i2,nPAT] := 0;
};
```

Scripting

Pattern Generation

Script (generation loop)

```
repeat {
  solve Cutting_Opt;
  let {i in WIDTHS} price[i] := Fill[i].dual;
  solve Pattern_Gen;
  printf "\n%7.2f%11.2e  ", Number, Reduced_Cost;
  if Reduced_Cost < -0.00001 then {
    let nPAT := nPAT + 1;
    let {i in WIDTHS} nbr[i,nPAT] := Use[i];
  }
  else break;
  for {i in WIDTHS} printf "%3i", Use[i];
};
```

Scripting

Pattern Generation

Script (final integer solution)

```
option Cutting_Opt.relax_integrality 0;
option Cutting_Opt.presolve 10;
solve Cutting_Opt;

if Cutting_Opt.result = "infeasible" then
    printf "\n*** No feasible integer solution ***\n\n";
else {
    printf "Best integer: %3i rolls\n\n", sum {j in 1..nPAT} Cut[j];
    for {j in 1..nPAT: Cut[j] > 0} {
        printf "%3i of:", Cut[j];
        printf {i in WIDTHS: nbr[i,j] > 0}: "%3i x %6.3f", nbr[i,j], i;
        printf "\n";
    }

    printf "\nWASTE = %5.2f%%\n\n",
        100 * (1 - (sum {i in WIDTHS} i * orders[i]) / (roll_width * Number));
}
```

Scripting

Pattern Generation

Results (relaxation)

```
ampl: include cutpatgen.run
```

```
20.44 -1.53e-01 1 3 2 0
18.78 -1.11e-01 0 1 3 0
18.37 -1.25e-01 0 1 0 3
17.96 -4.17e-02 0 6 0 1
17.94 -1.00e-06
```

Optimal relaxation: **17.9412 rolls**

```
10.0000 of: 1 x 6.770 3 x 7.560 2 x 17.460
4.3333 of: 1 x 7.560 3 x 17.460
3.1961 of: 1 x 7.560 3 x 18.760
0.4118 of: 6 x 7.560 1 x 18.760
```

WASTE = 2.02%

Scripting

Pattern Generation

Results (integer)

Rounded up to integer: **20 rolls**

Cut	10	5	4	1
6.77	1	0	0	0
7.56	3	1	1	6
17.46	2	3	0	0
18.76	0	0	3	1

WASTE = 12.10%

Best integer: **19 rolls**

Cut	10	5	3	1
6.77	1	0	0	0
7.56	3	1	1	6
17.46	2	3	0	0
18.76	0	0	3	1

WASTE = 7.48%

APIs (application programming interfaces)

Bring the modeling language to the programmer

- ❖ Data and result management in a general-purpose programming language
- ❖ Modeling and solving through calls to AMPL

Cutting Revisited

Hybrid approach

- ❖ Control & pattern creation from a programming language
 - * Pattern enumeration: finding all patterns
 - * Pattern generation: solving knapsack problems
- ❖ Model & modeling commands in AMPL

Choice of programming languages

- ❖ Java, MATLAB, C++

Key to program examples

- ❖ AMPL entities
- ❖ objects
- ❖ methods for working with AMPL
- ❖ functions

AMPL Model File

Basic pattern-cutting model

```
param nPatterns integer > 0;

set PATTERNS = 1..nPatterns; # patterns
set WIDTHS; # finished widths

param order {WIDTHS} >= 0; # rolls of width j ordered
param overrun; # permitted overrun on any width

param rolls {WIDTHS,PATTERNS} >= 0; # rolls of width i in pattern j

var Cut {PATTERNS} integer >= 0; # raw rolls to cut in each pattern

minimize TotalRawRolls: sum {p in PATTERNS} Cut[p];

subject to FinishedRollLimits {w in WIDTHS}:
    order[w] <= sum {p in PATTERNS} rolls[w,p] * Cut[p] <= order[w] + overrun;
```

Pattern Enumeration in MATLAB

Load & generate data, set up AMPL model

```
function cuttingEnum(dataFile)

% Get data from .mat file: roll_width, overrun, widths, orders
load(dataFile);

% Generate pattern matrix
[widthsDec,ind] = sort(widths,'descend');
patmat = patternEnum(roll_width,widthsDec);
patmat(:,ind) = patmat;

% Initialize and load cutting-stock model from file
AMPL = AMPL();
AMPL.read('cut.mod');
```

Pattern Enumeration in MATLAB

Send data to AMPL

```
% Send scalar values
AMPL.getParameter('overrun').setValues(overrun);
AMPL.getParameter('nPatterns').setValues(length(patmat));

% Send order vector
WidthOrder = DataFrame(1, 'WIDTHS', 'order');
WidthOrder.setColumn('WIDTHS', num2cell(widths));
WidthOrder.setColumn('order', orders);
AMPL.setData(WidthOrder, 'WIDTHS');

% Send pattern matrix
AllPatterns = DataFrame(2, 'WIDTHS', 'PATTERNS', 'rolls');
AllPatterns.setMatrix('patmat', num2cell(widths), num2cell(1:length(patmat)));
AMPL.setData(AllPatterns)
```

Pattern Enumeration in MATLAB

Solve and report

```
% Solve
ampl.setOption('solver' , 'gurobi');
ampl.solve

% Retrieve solution
CuttingPlan = ampl.getVariable('Cut').getValues();
cutvec = CuttingPlan.getColumnAsDoubles('val');

% Display solution
cuttingPlot (roll_width, widths, patmat(cutvec>0,:), cutvec(cutvec>0))
```

Pattern Enumeration in MATLAB

Enumeration routine

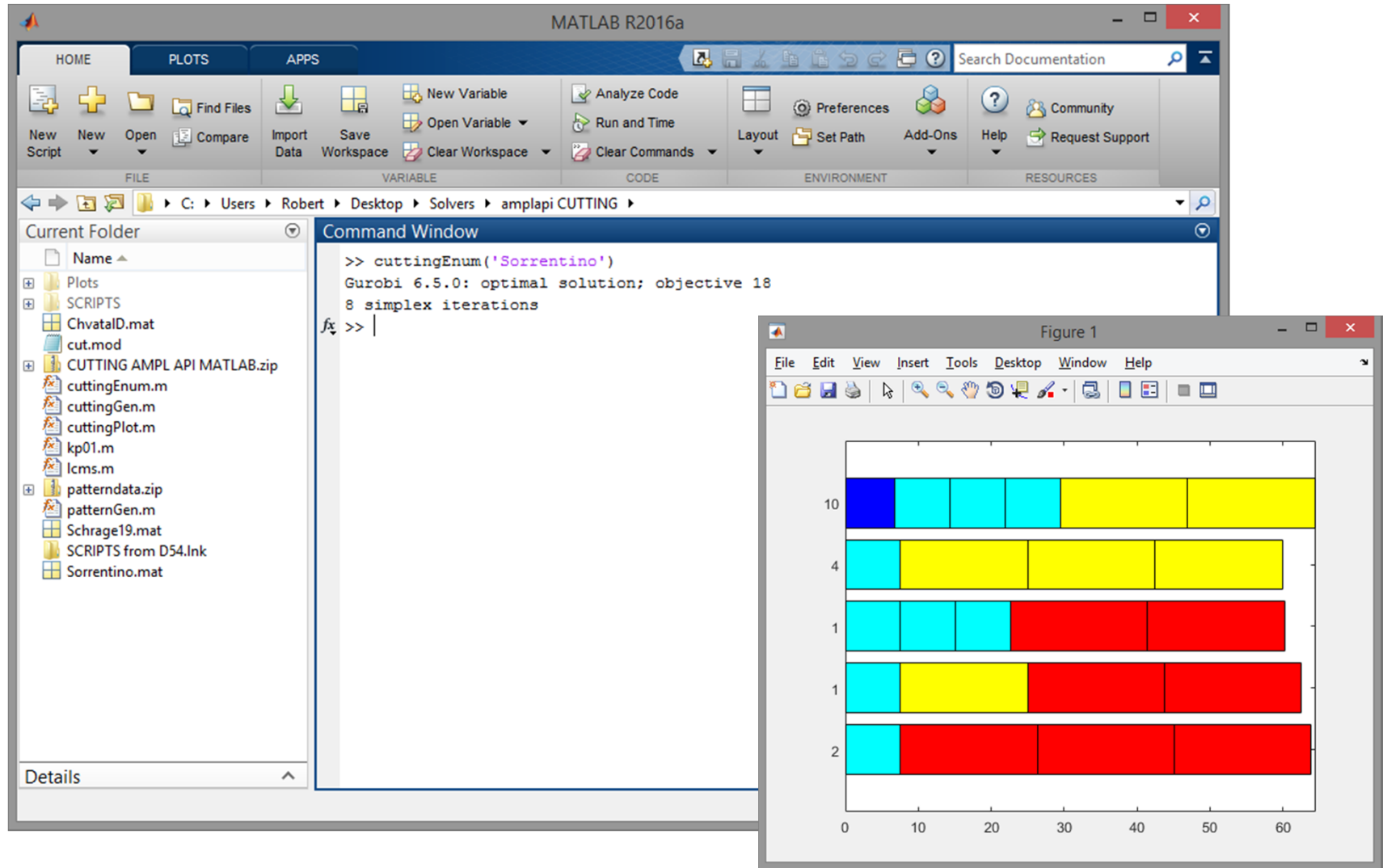
```
function patmat = patternEnum(rollwidth,widths)
if length(widths) == 1
    patmat = floor(rollwidth/widths(1));
else
    patmat = [];
    for n = floor(rollwidth/widths(1)):-1:0
        patnew = patternEnum (rollwidth-n*widths(1), widths(2:end));
        patmat = [patmat; n*ones(size(patnew,1),1) patnew];
    end
end
```

Pattern Enumeration in MATLAB

Plotting routine

```
function cuttingPlot (roll_width,widths,patmat,cutvec)
plotmat = zeros(length(cutvec),sum(max(patmat)));
colors = jet(length(widths));
plotpos = 0;
for j = 1:length(widths)
    for i = 1:length(cutvec)
        plotmat(i,plotpos+1:plotpos+patmat(i,j)) = widths(j);
    end
    for i = 1:max(patmat(:,j))
        colormat(plotpos+i,:) = colors(j,:);
    end
    plotpos = plotpos + max(patmat(:,j));
end
colormap(colormat); shading faceted
h = barh(plotmat,'stacked');
set (h, 'edgecolor','black'); set(gca,'YTickLabel',num2cell(cutvec))
xlim([0,roll_width]); ylim([0,numel(get(gca,'YTick'))+1])
```

Pattern Enumeration in MATLAB



Pattern Enumeration in Java

Generate patterns, set up AMPL model

```
public static void main(String[] args) throws IOException {
    import static com.ampl.examples.CuttingStock.Sorrentino;
    int[] sortedWidths = widths.clone();
    sortDescending(sortedWidths);
    ArrayList<Integer> patterns = new ArrayList<>();
    patternEnum (roll_width, sortedWidths, 0, patterns);

    // Initialize and load cutting-stock model from file
    AMPL ampl = new AMPL();
    try {
        ampl.read("cut.mod");
    }
}
```

Pattern Enumeration in Java

Send data to AMPL

```
ampl.getParameter("overrun").setValues(overrun);
int numPatterns = patterns.size() / widths.length;
ampl.getParameter("nPatterns").setValues(numPatterns);

DataFrame widthOrder = new DataFrame(1, "WIDTHS", "order");
widthOrder.setColumn("WIDTHS", widths);
widthOrder.setColumn("order", orders);
ampl.setData(widthOrder, true);

DataFrame allPatterns = new DataFrame(2, "WIDTHS", "PATTERNS", "rolls");
for (int i = 0; i < widths.length; i++) {
    for (int j = 0; j < numPatterns; j++) {
        allPatterns.addRow(
            sortedWidths[i], j + 1, patterns.get(j * widths.length + i));
    }
}
ampl.setData(allPatterns, false);
```

Pattern Enumeration in Java

Solve and report solution

```
    ampl.setOption("solver", "gurobi");  
    ampl.solve();  
    printSolution (ampl.getVariable("Cut"), ampl.getParameter("rolls"));  
} finally {  
    ampl.close();  
}  
}
```

In practice . . .

Integrate within a larger scheme

Retain benefits of algebraic modeling

- ❖ work with natural representation of optimization models
- ❖ efficient prototyping, reliable maintenance

Use the best tools for each part of the project

- ❖ program data manipulation in your choice of language
- ❖ work with optimization models in AMPL

Pattern Generation in MATLAB

Set up AMPL, get data

```
function cuttingGen(dataFile)

% Initialize
AMPL = AMPL();

% Load cutting-stock model from file
AMPL.read('cut.mod');
Cut = AMPL.getVariable('Cut');
Limits = AMPL.getConstraint('FinishedRollLimits');

% Get data from .mat file: roll_width, overrun, widths, orders
load(dataFile);
```

Pattern Generation in MATLAB

Send data to AMPL

```
% Send scalar values
```

```
AMPL.getParameter('overrun').setValues(overrun);  
AMPL.getParameter('nPatterns').setValues(length(widths));
```

```
% Send order vector
```

```
WidthOrder = DataFrame(1, 'WIDTHS', 'order');  
WidthOrder.setColumn('WIDTHS', num2cell(widths));  
WidthOrder.setColumn('order', orders);  
AMPL.setData(WidthOrder, 'WIDTHS');
```

```
% Generate and send initial pattern matrix
```

```
maxpat = floor(roll_width./widths);  
patmat = diag(maxpat);  
InitPatterns = DataFrame(2, 'WIDTHS', 'PATTERNS', 'rolls');  
InitPatterns.setMatrix(patmat, num2cell(widths), num2cell(1:length(widths)));  
AMPL.setData(InitPatterns);
```

Pattern Generation in MATLAB

Set up for generation loop

```
% Set solve options
AMPL.setOption('solver','gurobi');
AMPL.setOption('relax_integrality','1');

% Set up DataFrame for sending AMPL new patterns
AMPL.eval('param newpat {WIDTHS} integer >= 0;');
NewPattern = DataFrame(1, 'WIDTHS', 'newpat');
NewPattern.setColumn('WIDTHS', num2cell(widths));

% Compute multiplier for integer weights
[n,d] = rat(widths);
intmult = lcm(d);
```

Pattern Generation in MATLAB

Loop 1: Retrieve duals & look for new pattern

```
while 1
    ampl.solve
    DualPrices = Limits.getValues;
    dualvec = DualPrices.getColumnAsDoubles('dual');
    wgt = []; val = [];
    for w = 1:length(widths)
        if dualvec(w) > 0
            wgt = [wgt widths(w)*ones(1,maxpat(w))];
            val = [val dualvec(w)*ones(1,maxpat(w))];
        end
    end
    % Solve knapsack problem for potential new pattern
    [kmax,z] = kp01 (round(intmult*wgt), val, intmult*roll_width);
    if kmax < 1.000001
        break;
    end
end
```


Pattern Generation in MATLAB

Loop 2: Send new pattern to AMPL

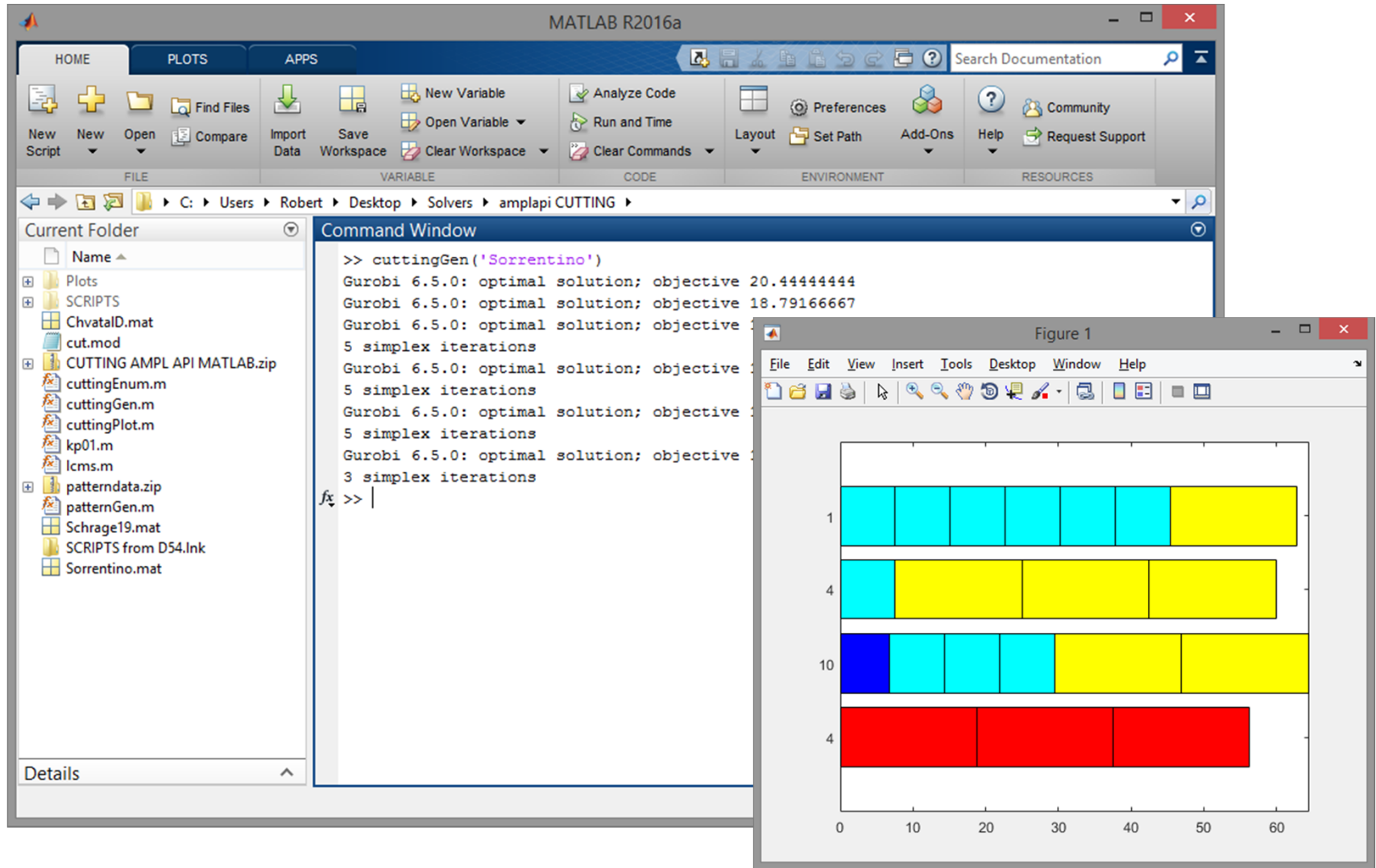
```
widthlist = wgt(z);
for w = 1:length(widths)
    newpat(w) = length(find(widthlist==widths(w)));
end
patmat = [patmat; newpat];
NewPattern.setColumn('newpat', newpat);
ampl.setData(NewPattern);

ampl.eval('let nPatterns := nPatterns + 1;');
ampl.eval('let {w in WIDTHS} rolls[w,nPatterns] := newpat[w];');
end

% Compute and display integer solution
ampl.setOption('relax_integrality','0');
ampl.solve;

CuttingPlan = Cut.getValues();
cutvec = CuttingPlan.getColumnAsDoubles('val');
cuttingPlot (roll_width, widths, patmat(cutvec>0,:), cutvec(cutvec>0))
```

Pattern Generation in MATLAB



In practice . . .

Implement hybrid iterative schemes

- ❖ build powerful software for hard problems

Alternate between optimization & other analytics

- ❖ invoke specialized optimizers for subproblems

Data Transfer: **Alternatives**

Process

- ❖ Define symbolic sets & parameters in AMPL model
- ❖ Create corresponding objects in program
- ❖ Transfer data using API methods
 - * Program to AMPL
 - * AMPL to program

Methods for transfer between . . .

- ❖ Scalar values
- ❖ Collections of values
 - * AMPL indexed expressions
 - * Java arrays, MATLAB matrices
- ❖ Relational tables
 - * AMPL “table” structures
 - * API DataFrame objects in Java, MATLAB

AMPL API

Availability

AMPL API version 1.2 released

- ❖ Java, MATLAB, C++ (beta)
- ❖ Add-ons to all AMPL distributions
- ❖ Download from www.ampl.com/products/api/

More languages to follow

- ❖ Python
- ❖ R
- ❖ .NET: C#, Visual Basic

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By using a high-level representation that represents optimization models in the same ways that people think about them, AMPL promotes rapid development and reliable results.
AMPL integrates a modeling language for describing optimization data, variables, objectives, and constraints; a command language for browsing models and analyzing results; and a scripting language for gathering and manipulating data and for implementing iterative

WHAT'S NEW?
March 6-8
6th INFORMS Optimization Society Conference, Houston, Texas.
AMPL sponsorship of this event & table in the exhibit area

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