Model-Based Optimization + Application Programming = Streamlined Deployment in AMPL

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Examples

Model-based optimization

- Model-based vs. Method-based *approaches*
 - * Example: Balanced assignment
- Declarative vs. Executable *modeling languages*
 - * Example: AMPL vs. gurobipy for multicommodity flow

Examples

Model-based optimization

Application programming

- Extending a modeling language with scripting
 - * Example: Tradeoffs between roll-cutting objectives

Examples

Model-based optimization

Application programming

Streamlined deployment

- Modeling language APIs
 - * Example: Pattern enumeration in Python and R
- Python integration
 - * Example: Python data embedded in an AMPL model
 - * Example: Custom stopping criteria using Gurobi callbacks
 - * Example: Executing Python inside AMPL
- ✤ AMPL in Jupyter notebooks
 - * Example: Mixed AMPL and Python notebooks
- Building a decision-making tool for deployment
 - ***** Example: QuanDec

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Model-Based vs. Method-Based Approaches to Optimization

Example: Balanced Assignment

meeting of employees from around the world

Given

- several employee categories (title, location, department, male/female)
- ✤ a specified number of project groups

Assign

✤ each employee to a project group

So that

- $\boldsymbol{\ast}$ the groups have about the same size
- the groups are as "diverse" as possible with respect to all categories

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Balanced Assignment

Method-Based Approach

Define an algorithm to build a balanced assignment

- Start with all groups empty
- Make a list of people (employees)
- For each person in the list:
 - * Add to the group whose resulting "sameness" will be least

```
Initialize all groups G = { }
Repeat for each person p
  sMin = Infinity
Repeat for each group G
    s = total "sameness" in G ∪ {p}
    if s < sMin then
       sMin = s
       GMin = G
Assign person p to group GMin</pre>
```

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Balanced Assignment Method-Based Approach (cont'd)

Define a computable concept of "sameness"

- Sameness of any two people:
 - * Number of categories in which they are the same
- Sameness of a group:
 - * Sum of the sameness of all pairs of people in the group

Refine the algorithm to get better results

- Reorder the list of people
- Locally improve the initial "greedy" solution by swapping group members
- Seek further improvement through local search metaheuristics
 - * What are the neighbors of an assignment?
 - * How can two assignments combine to create a better one?

Balanced Assignment

Model-Based Approach

Formulate a "minimal sameness" model

- Define decision variables for assignment of people to groups
 - * $x_{ij} = 1$ if person 1 assigned to group *j*
 - * $x_{ij} = 0$ otherwise
- Specify valid assignments through constraints on the variables
- Formulate sameness as an objective to be minimized
 ** Total sameness* = sum of the sameness of all groups

Send to an off-the-shelf solver

- Choice of excellent solvers
- Broad problem classes handled efficiently
- Special cases recognized and exploited to advantage
 - * zero-one variables like x_{ij}

Balanced Assignment Model-Based Formulation

Given

- *P* set of people
- *C* set of categories of people
- t_{ik} type of person *i* within category *k*, for all $i \in P, k \in C$

and

- *G* number of groups
- g^{\min} lower limit on people in a group
- g^{\max} upper limit on people in a group

Define

$$\begin{split} s_{i_1i_2} &= |\{k \in C \colon t_{i_1k} = t_{i_2k}\}|, \text{ for all } i_1 \in P, i_2 \in P\\ sameness \ of \ persons \ i_1 \ and \ i_2 \end{split}$$

Balanced Assignment Model-Based Formulation (cont'd)

Determine

 $\begin{aligned} x_{ij} \in \{0,1\} &= 1 \text{ if person } i \text{ is assigned to group } j \\ &= 0 \text{ otherwise, for all } i \in P, j = 1, \dots, G \end{aligned}$

To minimize

 $\sum_{i_1 \in P} \sum_{i_2 \in P} s_{i_1 i_2} \sum_{j=1}^G x_{i_1 j} x_{i_2 j}$ total sameness of all pairs of people in all groups

Subject to

 $\sum_{j=1}^{G} x_{ij} = 1$, for each $i \in P$

each person must be assigned to one group

 $g^{\min} \leq \sum_{i \in P} x_{ij} \leq g^{\max}$, for each $j = 1, \dots, G$

each group must be assigned an acceptable number of people

Balanced Assignment Model-Based Solution

Optimize with an off-the-shelf solver

Choose among many alternatives

- Linearize and send to a mixed-integer linear solver
 * CPLEX, Gurobi, Xpress; CBC, MIPCL, SCIP
- Send quadratic formulation to a mixed-integer solver that automatically linearizes products involving binary variables
 * CPLEX, Gurobi, Xpress
- Send quadratic formulation to a nonlinear solver
 - * Mixed-integer nonlinear: Knitro, BARON
 - * Continuous nonlinear (might come out integer): MINOS, Ipopt, ...

Model-Based vs. Method-Based

Where is the work?

- * *Method-based:* Programming an implementation of the method
- * *Model-based:* Constructing a formulation of the model

Which should you prefer?

- ✤ For simple problems, any approach can seem pretty easy
- ✤ But real optimization problems are seldom simple . . .

Complications in Balanced Assignment

"Total Sameness" is problematical

- ✤ Hard for client to relate to goal of diversity
- ✤ Minimize "total variation" instead
 - * Sum over all types: most minus least assigned to any group

Client has special requirements

- No employee should be "isolated" within their group
 - * No group can have exactly one woman
 - Every person must have a group-mate from the same location and of equal or adjacent rank

Room capacities are variable

- Different groups have different size limits
- Minimize "total deviation"
 - * Sum over all types: greatest violation of target range for any group

Revise or replace the solution approach

- Total variation is less suitable to a greedy algorithm
- Total variation is harder to locally improve
- Client constraints are challenging to enforce

Update or re-implement the method

 Even small changes to the problem can necessitate major changes to the method and its implementation

Replace the objective

Formulate additional constraints

Send back to the solver

To write new objective, add variables

 $\begin{array}{l} y_{kl}^{\min} & \text{fewest people of category } k, \text{type } l \text{ in any group,} \\ y_{kl}^{\max} & \text{most people of category } k, \text{type } l \text{ in any group,} \\ & \text{for each } k \in C, l \in T_k = \bigcup_{i \in P} \{t_{ik}\} \end{array}$

Add defining constraints

$$y_{kl}^{\min} \leq \sum_{i \in P: t_{ik}=l} x_{ij}, \text{ for each } j = 1, \dots, G; \ k \in C, l \in T_k$$
$$y_{kl}^{\max} \geq \sum_{i \in P: t_{ik}=l} x_{ij}, \text{ for each } j = 1, \dots, G; \ k \in C, l \in T_k$$

Minimize total variation

 $\sum_{k \in C} \sum_{l \in T_k} (y_{kl}^{\max} - y_{kl}^{\min})$

To express client requirement for women in a group, let $Q = \{i \in P: t_{i,m/f} = female\}$

Add constraints

 $\sum_{i \in Q} x_{ij} = 0$ or $\sum_{i \in Q} x_{ij} \ge 2$, for each $j = 1, \dots, G$

To express client requirement for women in a group, let $Q = \{i \in P: t_{i,m/f} = female\}$ Define logic variables

 $z_j \in \{0,1\} = 1$ if any women assigned to group j= 0 otherwise, for all j = 1, ..., G

Add constraints relating logic variables to assignment variables

$$\begin{aligned} z_j &= 0 \ \Rightarrow \sum_{i \in Q} x_{ij} = 0, \\ z_j &= 1 \ \Rightarrow \sum_{i \in Q} x_{ij} \ge 2, \text{ for each } j = 1, \dots, G \end{aligned}$$

To express client requirement for women in a group, let $Q = \{i \in P: t_{i,m/f} = \text{female}\}$ Define logic variables $z_j \in \{0,1\} = 1$ if any women assigned to group j

= 0 otherwise, for all $j = 1, \ldots, G$

Linearize constraints relating logic variables to assignment variables

 $2z_j \leq \sum_{i \in Q} x_{ij} \leq |Q| z_j$, for each $j = 1, \dots, G$

Method-Based Remains Popular for ...

Heuristic approaches

- ✤ Simple heuristics
 - * Greedy algorithms, local improvement methods
- Metaheuristics
 - * Evolutionary methods, simulated annealing, tabu search, GRASP, ...

Situations hard to formulate mathematically

- Difficult combinatorial constraints
- Black-box objectives and constraints

Large-scale, intensive applications

- Routing fleets of delivery trucks
- Finding shortest routes in mapping apps

... and it appeals to programmers

Model-Based Has Become Common for ...

Diverse application areas (active AMPL users)

- ✤ Energy and Utilities
 - * power networks, gas pipelines, hydroelectric power, water distribution
- ✤ Industry
 - * mining, steel, chemicals, oil refining, forestry and paper
 - * cars & trucks, paper products, processed foods
- ✤ Transportation
 - ***** airlines, trucking
- Services
 - * supply chain, hospitals & medicine, construction management
- Communications
 - * telecommunications, social media, cloud computing, distribution
- ✤ Finance
 - * software tools, investment management, commodity management
- ✤ Advanced Technologies
 - * artificial intelligence, distributed computing, biotechnology

Model-Based Has Become Common for ...

Diverse application areas

Diverse fields

- Operations research & management science
- ✤ Business analytics
- Engineering & science
- Economics & finance

Model-Based Has Become Common for ...

Diverse industries

Diverse fields

Diverse kinds of users

- Anyone who took an "optimization" class
- ✤ Anyone else with a technical background
- Newcomers to optimization

These have in common . . .

- Users inclined toward modeling; focus is
 - * more on *what* should be solved
 - * less on *how* it should be solved
- ✤ Good algebraic formulations for off-the-shelf solvers

Trends Favor Model-Based Optimization

Model-based approaches have spread

- Model-based metaheuristics ("Matheuristics")
- Solvers for SAT, planning, constraint programing

Off-the-shelf optimization solvers have kept improving

- ✤ Solve the same problems faster and faster
- Handle broader problem classes
- Recognize special cases automatically

Optimization models have become easier to embed within broader methods

- Model-based evolution of solver APIs
- ✤ APIs for optimization modeling systems

Modeling Languages for Model-Based Optimization

Background

- ✤ The modeling lifecycle
- Modeling languages
- ✤ Algebraic modeling languages

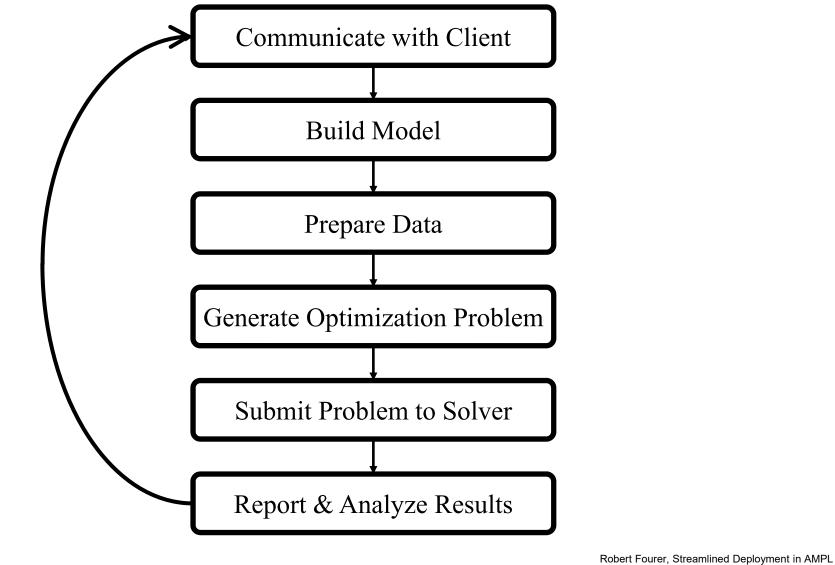
Design approaches

- Matrix generators vs. modeling languages
- Declarative vs. executable modeling languages

Example: AMPL vs. gurobipy

Example: Balanced Assignment in AMPL

The Optimization Modeling Lifecycle



Managing the Modeling Lifecycle

Goals for optimization software

- ✤ Repeat the cycle quickly and reliably
- ✤ Get results before client loses interest
- Deploy for application

Complication: two forms of an optimization problem

- Modeler's form
 - * Mathematical description, easy for people to work with
- Solver's form
 - * Explicit data structure, easy for solvers to compute with

Challenge: translate between these two forms

Modeling Languages

Describe your model

- Write your symbolic model in a computer-readable modeler's form
- Prepare data for the model
- Let computer translate to & from the solver's form

Limited drawbacks

- Separate language to be learned
- Overhead in translation to algorithm's form
- Confidential formulation to be protected

Great advantages

- ✤ Faster modeling cycles
- ✤ More reliable modeling
- More maintainable applications

Designed for a model-based approach

- Define data in terms of sets & parameters
 * Analogous to database keys & records
- Define decision variables
- Minimize or maximize an algebraic function of decision variables
- Subject to algebraic equations or inequalities that constrain the values of the variables

Advantages

- ✤ Familiar
- Powerful
- Proven



Algebraic modeling language and system

- Built specially for optimization
- Designed to support many solvers

Design goals

- Powerful, general expressions
- Natural, easy-to-learn modeling principles
- ✤ Efficient processing that scales well with problem size

Executable vs. Declarative Modeling Languages for Optimization

Example: Two representative widely used systems

Executable: gurobipy

- Python modeling interface for Gurobi solver
- http://gurobi.com

Declarative: 👗 AMPL

- Specialized modeling language with multi-solver support
- http://ampl.com

Executable

Concept

- Create an algebraic modeling language inside a general-purpose programming language
- Redefine operators like + and <=
 to return constraint objects rather than simple values

Advantages

- ✤ Ready integration with applications
- Good access to advanced solver features

Disadvantages

- Programming issues complicate description of the model
- Modeling and programming bugs are hard to separate
- Efficiency issues are more of a concern

Declarative

Concept

- ✤ Design a language specifically for optimization modeling
 - * Resembles mathematical notation as much as possible
- Extend to command scripts and database links
- Connect to external applications via APIs

Disadvantages

- ✤ Adds a system between application and solver
- Does not have a full object-oriented programming framework

Advantages

- Streamlines model development
- Promotes validation and maintenance of models
- Can provide APIs for many popular programming languages

Comparison: Executable vs. Declarative

Example: Multicommodity Flow

ship multiple goods over a network

Given

- ✤ networks nodes and arc
- supplies or demands at the nodes
- ✤ capacities on the arcs

Determine

how much to ship over each arc

So that

- demands are met by the supplies
- * shipping costs are minimized

Comparison Data

gurobipy

 Assign values to Python lists and dictionaries

AMPL

 Define symbolic model sets and parameters

set COMMODITIES;
set NODES;

```
set ARCS within {NODES,NODES};
param capacity {ARCS} >= 0;
```

```
set COMMODITIES := Pencils Pens ;
set NODES := Detroit Denver
Boston 'New York' Seattle ;
param: ARCS: capacity:
    Boston 'New York' Seattle :=
Detroit 100 80 120
Denver 120 120 120 ;
```

Comparison Data (cont'd)

gurobipy

<pre>'Detroit'): 'Denver'): 'Boston'): 'New York'):</pre>	50, 60, -50, -50,
	•
'Seattle'):	-10,
'Detroit'):	60,
'Denver'):	40,
'Boston'):	-40,
'New York'):	-30,
'Seattle'):	-30 }
	<pre>'Denver'): 'Boston'): 'New York'): 'Seattle'): 'Detroit'): 'Denver'): 'Boston'): 'New York'):</pre>

AMPL

param inflow {COMMODITIES,NODES};

param inflow	(tr):		
1 - 1 1	Pencils	Pens	:=
Detroit	50	60	
Denver	60	40	
Boston	-50	-40	
'New York'	-50	-30	
Seattle	-10	-30	;
1			

Comparison Data (cont'd) gurobipy

<pre>cost = { ('Pencils',</pre>	'Detroit',	'Boston'):	10,
('Pencils',	'Detroit',	'New York'):	20,
('Pencils',	'Detroit',	'Seattle'):	60,
('Pencils',	'Denver',	'Boston'):	40,
('Pencils',	'Denver',	'New York'):	40,
('Pencils',	'Denver',	'Seattle'):	30,
('Pens',	'Detroit',	'Boston'):	20,
('Pens',	'Detroit',	'New York'):	20,
('Pens',	'Detroit',	'Seattle'):	80,
('Pens',	'Denver',	'Boston'):	60,
('Pens',	'Denver',	'New York'):	70,
('Pens',	'Denver',	'Seattle'):	30 }

Comparison

Data (cont'd)

AMPL

param cost {COMMODITIES,ARCS} >= 0;

```
param cost
 [Pencils,*,*] (tr) Detroit Denver :=
    Boston
                     10
                             40
    'New York'
                     20
                             40
                     60
    Seattle
                             30
 [Pens,*,*] (tr) Detroit Denver :=
    Boston
                     20
                             60
    'New York'
                     20
                             70
    Seattle
                     80
                             30
                                  ;
```

Comparison Model

gurobipy

```
m = Model('netflow')
flow = m.addVars(commodities, arcs, obj=cost, name="flow")
m.addConstrs(
  (flow.sum('*',i,j) <= capacity[i,j] for i,j in arcs), "cap")
m.addConstrs(
  (flow.sum(h,'*',j) + inflow[h,j] == flow.sum(h,j,'*')
      for h in commodities for j in nodes), "node")</pre>
```

Comparison (Note on Summations)

gurobipy quicksum

```
m.addConstrs(
```

```
(quicksum(flow[h,i,j] for i,j in arcs.select('*',j)) + inflow[h,j] ==
quicksum(flow[h,j,k] for j,k in arcs.select(j,'*'))
for h in commodities for j in nodes), "node")
```

quicksum (data)

A version of the Python sum function that is much more efficient for building large Gurobi expressions (LinExpr or QuadExpr objects). The function takes a list of terms as its argument.

Note that while quicksum is much faster than sum, it isn't the fastest approach for building a large expression. Use addTerms or the LinExpr() constructor if you want the quickest possible expression construction.

Comparison Model (cont'd)

```
var Flow {COMMODITIES,ARCS} >= 0;
minimize TotalCost:
    sum {h in COMMODITIES, (i,j) in ARCS} cost[h,i,j] * Flow[h,i,j];
subject to Capacity {(i,j) in ARCS}:
    sum {h in COMMODITIES} Flow[h,i,j] <= capacity[i,j];
subject to Conservation {h in COMMODITIES, j in NODES}:
    sum {(i,j) in ARCS} Flow[h,i,j] + inflow[h,j] =
    sum {(j,i) in ARCS} Flow[h,j,i];
```

Comparison Solution

gurobipy

```
m.optimize()
if m.status == GRB.Status.OPTIMAL:
    solution = m.getAttr('x', flow)
    for h in commodities:
        print('\nOptimal flows for %s:' % h)
        for i,j in arcs:
            if solution[h,i,j] > 0:
                print('%s -> %s: %g' % (i, j, solution[h,i,j]))
```

Solved in 0 iterations and 0.00 seconds Optimal objective 5.50000000e+03

Optimal flows for Pencils: Detroit -> Boston: 50 Denver -> New York: 50 Denver -> Seattle: 10 Optimal flows for Pens: ...

Comparison **Solution** (cont'd)

```
ampl: solve;
Gurobi 8.1.0: optimal solution; objective 5500
2 simplex iterations
ampl: display Flow;
Flow [Pencils,*,*]
       Boston 'New York' Seattle :=
:
           0
                   50
                            10
Denver
Detroit 50
                    0
                             0
 [Pens,*,*]
       Boston 'New York' Seattle
                                    :=
Denver
          10
                    0
                            30
Detroit 30
                   30
                             0
;
```

Comparison

Integration with Solvers

gurobipy

- Works closely with the Gurobi solver: callbacks during optimization, fast re-solves after problem changes
- Offers convenient extended expressions: min/max, and/or, if-then-else

- Supports all popular solvers
- Extends to general nonlinear and logic expressions
 - * Connects to nonlinear function libraries and user-defined functions
- Automatically computes nonlinear function derivatives

Comparison

Integration with Applications

gurobipy

- Everything can be developed in Python
 - * Extensive data, visualization, deployment tools available
- ✤ Limited modeling features also in C++, C#, Java

- Modeling language extended with loops, tests, assignments
- Application programming interfaces (APIs) for calling AMPL from C++, C#, Java, MATLAB, Python, R
 - * Efficient methods for data interchange
- Add-ons for streamlined deployment
 - * QuanDec by Cassotis
 - * Opalytics Cloud Platform

Balanced Assignment Revisited

Given

- *P* set of people
- *C* set of categories of people
- t_{ik} type of person *i* within category *k*, for all $i \in P, k \in C$

and

- *G* number of groups
- g^{\min} lower limit on people in a group
- g^{\max} upper limit on people in a group

Define

 $T_k = \bigcup_{i \in P} \{t_{ik}\}, \text{ for all } k \in C$

set of all types of people in category k

Balanced Assignment Revisited in AMPL

Sets, parameters

Balanced Assignment

Determine

 $\begin{aligned} x_{ij} \in \{0,1\} &= 1 \text{ if person } i \text{ is assigned to group } j \\ &= 0 \text{ otherwise, for all } i \in P, j = 1, \dots, G \\ y_{kl}^{\min} & \text{fewest people of category } k, \text{ type } l \text{ in any group,} \\ y_{kl}^{\max} & \text{most people of category } k, \text{ type } l \text{ in any group,} \\ & \text{for each } k \in C, l \in T_k \end{aligned}$

Where

 $y_{kl}^{\min} \leq \sum_{i \in P: t_{ik}=l} x_{ij}, \text{ for each } j = 1, \dots, G; \ k \in C, l \in T_k$ $y_{kl}^{\max} \geq \sum_{i \in P: t_{ik}=l} x_{ij}, \text{ for each } j = 1, \dots, G; \ k \in C, l \in T_k$

Balanced Assignment in AMPL

Variables, defining constraints

```
var Assign {i in PEOPLE, j in 1..numberGrps} binary;
              # Assign[i,j] is 1 if and only if
              # person i is assigned to group j
var MinType {k in CATEG, TYPES[k]};
var MaxType {k in CATEG, TYPES[k]};
              # fewest and most people of each type, over all groups
subj to MinTypeDefn {j in 1..numberGrps, k in CATEG, l in TYPES[k]}:
  MinType[k,l] <= sum {i in PEOPLE: type[i,k] = l} Assign[i,j];</pre>
subj to MaxTypeDefn {j in 1..numberGrps, k in CATEG, l in TYPES[k]}:
   MaxType[k,1] >= sum {i in PEOPLE: type[i,k] = 1} Assign[i,j];
              # values of MinTypeDefn and MaxTypeDefn variables
              # must be consistent with values of Assign variables
```

```
y_{kl}^{\max} \ge \sum_{i \in P: t_{ik}=l} x_{ij}, for each j = 1, \dots, G; k \in C, l \in T_k
```

Balanced Assignment

Minimize

 $\sum_{k \in C} \sum_{l \in T_k} (y_{kl}^{\max} - y_{kl}^{\min})$

sum of inter-group variation over all types in all categories

Subject to

 $\sum_{j=1}^{G} x_{ij} = 1$, for each $i \in P$

each person must be assigned to one group

 $g^{\min} \leq \sum_{i \in P} x_{ij} \leq g^{\max}$, for each $j = 1, \dots, G$

each group must be assigned an acceptable number of people

Balanced Assignment in AMPL

Objective, assignment constraints

$$g^{\min} \leq \sum_{i \in P} x_{ij} \leq g^{\max}$$
, for each $j = 1, \dots, G$

Balanced Assignment

Define also

 $Q = \{i \in P : t_{i,m/f} = \text{female}\}$

Determine

 $z_j \in \{0,1\} = 1$ if any women assigned to group j= 0 otherwise, for all j = 1, ..., G

Subject to

 $\begin{aligned} 2z_j &\leq \sum_{i \in Q} x_{ij} \leq |Q| \, z_j, \text{ for each } j = 1, \dots, G \\ each \, group \, must \, have \, either \\ no \, women \, (z_j = 0) \, or \geq 2 \, women \, (z_j = 1) \end{aligned}$

Balanced Assignment in AMPL

Supplemental constraints

```
set WOMEN = {i in PEOPLE: type[i,'m/f'] = 'F'};
```

```
var WomenInGroup {j in 1..numberGrps} binary;
```

```
subj to Min2WomenInGroupLO {j in 1..numberGrps}:
    2 * WomenInGroup[j] <= sum {i in WOMEN} Assign[i,j];</pre>
```

```
subj to Min2WomenInGroupUP {j in 1..numberGrps}:
    sum {i in WOMEN} Assign[i,j] <= card(WOMEN) * WomenInGroup[j];</pre>
```

$$2z_j \leq \sum_{i \in Q} x_{ij} \leq |Q| z_j$$
, for each $j = 1, \dots, G$

Balanced Assignment Modeling Language Data

210 people

set PH	EOPLE :=	:								
BIV	V AJH	FWI	IGN	KWR	KKI	HMN	SML	RSR	TBR	
KRS	S CAE	MPO	CAR	PSL	BCG	DJA	AJT	JPY	HWG	
TLF	r Mrl	JDS	JAE	TEN	MKA	NMA	PAS	DLD	SCG	
AV A		GCY	OGZ	SME	KKA	MMY	API	ASA	JLN	
JR	C SJO	WMS	RLN	WLB	SGA	MRE	SDN	HAN	JSG	
AMF	r dhy	JMS	AGI	RHE	BLE	SMA	BAN	JAP	HER	
MES	S DHE	SWS	ACI	RJY	TWD	MMA	JJR	MFR	LHS	
JAI) CWU	PMY	CAH	SJH	EGR	JMQ	GGH	MMH	JWR	
MJF		WAD	LVN	DHR	ABE	LSR	MBT	AJU	SAS	
JRS	S RFS	TAR	DLT	HJO	SCR	CMY	GDE	MSL	CGS	
HCN		RPR	RCR	RLS	DSF	MNA	MSR	PSY	MET	
		PWS	CTS	KLN	RDN	ANV	LMN	FSM	KWN	
CW1		EJD	AJS	SBK	JWB	SNN	PST	PSZ	AWN	
		CPR	NHI	HKA	VMA	DMN	KRA	CSN	HRR	
SWF		AVI	RHA	KWY	MLE	FJL	ES0	TJY	WHF	
		MTH	RMN	WFS	CEH	SOL	ASO	MDI	RGE	
		CGH	RHD	MBM	MRH	RGF	PSA	TTI	HMG	
EC4		MKN	SBM	RCG	JMA	EGL	UJT	ETN	GWZ	
MA]		HFE	PSO	APT	JMT	RJE	MRZ	MRK	XYF	
JCC		SCS	RDL	TMN	CGY	GMR	SER	RMS	JEN	
DWC	D REN	DGR	DET	FJT	RJZ	MBY	RSN	REZ	BLW	;

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Balanced Assignment Modeling Language Data

4 categories, 18 types, 12 groups, 16-19 people/group

```
set CATEG := dept loc 'm/f' title ;
param type:
               loc
                    'm/f' title
     dept
                                        :=
BIW
     NNE
           Peoria
                          М
                              Assistant
     WSW
KRS
           Springfield
                          F
                              Assistant
TLR
     NNW
           Peoria
                          F
                              Adjunct
     NNW
VAA
           Peoria
                          М
                              Deputy
JRT
     NNE
           Springfield
                          М
                              Deputy
     SSE
           Peoria
AMR
                          М
                              Deputy
MES
     NNE
           Peoria
                          М
                              Consultant
     NNE
           Peoria
JAD
                              Adjunct
                          М
MJR
     NNE
           Springfield
                          М
                              Assistant
JRS
     NNE
           Springfield
                          М
                              Assistant
HCN
     SSE
           Peoria
                          М
                              Deputy
DAN
     NNE
           Springfield
                          М
                              Adjunct
param numberGrps := 12 ;
param minInGrp := 16 ;
param maxInGrp := 19 ;
```

Balanced Assignment Modeling Language Solution

Model + *data* = *problem instance to be solved (CPLEX)*

```
ampl: model BalAssign.mod;
ampl: data BalAssign.dat;
ampl: option solver cplex;
ampl: option show_stats 1;
ampl: solve;
2568 variables:
        2532 binary variables
        36 linear variables
678 constraints, all linear; 26328 nonzeros
        210 equality constraints
        456 inequality constraints
        12 range constraints
1 linear objective; 36 nonzeros.
CPLEX 12.9.0.0: optimal integer solution; objective 16
23690 MIP simplex iterations
159 branch-and-bound nodes
                                                                7.4 sec
```

Balanced Assignment Modeling Language Solution

Model + *data* = *problem instance to be solved (Gurobi)*

```
ampl: model BalAssign.mod;
ampl: data BalAssign.dat;
ampl: option solver gurobi;
ampl: option show_stats 1;
ampl: solve;
2568 variables:
        2532 binary variables
        36 linear variables
678 constraints, all linear; 26328 nonzeros
        210 equality constraints
        456 inequality constraints
        12 range constraints
1 linear objective; 36 nonzeros.
Gurobi 8.1.0: optimal solution; objective 16
521639 simplex iterations
804 branch-and-cut nodes
                                                             109.1 sec
```

Extending a Modeling Language with Scripting

Example: Roll Cutting

fill orders for rolls of various widths

Given

- ✤ raw rolls of a large (fixed) width
- demands for various (smaller) ordered widths
- $\boldsymbol{\ast}\,$ a selection of cutting patterns that may be used

Determine

 $\boldsymbol{\ast}$ the number of times to cut each pattern

So that

- demands are met (or slightly exceeded)
- * raw rolls cut and wasted material are minimized

AMPL Model Mathematical Formulation

Given

- w width of "raw" rolls
- W set of (smaller) ordered widths
- *n* number of cutting patterns considered

and

- a_{ij} occurrences of width *i* in pattern *j*, for each $i \in W$ and j = 1, ..., n
- b_i orders for width i, for each $i \in W$
- *o* limit on overruns

AMPL Model Mathematical Formulation (cont'd)

Determine

 $\begin{array}{ll} X_j & \text{number of rolls to cut using pattern } j, \\ & \text{for each } j = 1, \dots, n \end{array}$

to minimize

 $\sum_{j=1}^{n} X_{j}$

total number of rolls cut

subject to

 $b_i \leq \sum_{j=1}^n a_{ij} X_j \leq b_i + o$, for all $i \in W$

number of rolls of width *i* cut must be at least the number ordered, and must be within the overrun limit

AMPL Model AMPL Formulation

Symbolic model

```
param rawWidth;
set WIDTHS;
param nPatterns integer > 0;
set PATTERNS = 1..nPatterns;
param rolls {WIDTHS,PATTERNS} >= 0, default 0;
param order {WIDTHS} >= 0;
param overrun;
var Cut {PATTERNS} integer >= 0;
minimize TotalCut: sum {p in PATTERNS} Cut[p];
subject to OrderLimits {w in WIDTHS}:
    order[w] <= sum {p in PATTERNS} rolls[w,p] * Cut[p] <= order[w] + overrun;</pre>
```

 $b_i \le \sum_{i=1}^n a_{ii} X_i \le b_i + o$

AMPL Model **AMPL Formulation** (cont'd)

Explicit data (independent of model)

```
param rawWidth := 64.5 ;
param: WIDTHS: order :=
    6.77   10
    7.56   40
    17.46   33
    18.76   10 ;
param nPatterns := 9 ;
param rolls: 1  2  3  4  5  6  7  8  9 :=
    6.77  0  1  1  0  3  2  0  1  4
    7.56  1  0  2  1  1  4  6  5  2
    17.46  0  1  0  2  1  0  1  1  1
    18.76  3  2  2  1  1  1  0  0  0;
param overrun := 6 ;
```

AMPL Model AMPL Command Language

Model + *data* = *problem instance to be solved*

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver cplex;
ampl: solve;
CPLEX 12.9.0.0: optimal integer solution; objective 20
3 MIP simplex iterations
0 branch-and-bound nodes
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13 7 4 9 3
```

AMPL Model **Command Language** (cont'd)

Solver choice independent of model and data

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver gurobi;
ampl: solve;
Gurobi 8.1.0: optimal solution; objective 20
3 simplex iterations
1 branch-and-cut nodes
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13 7 4 9 3
```

AMPL Model **Command Language** (cont'd)

Results available for browsing

```
ampl: display {p in PATTERNS} sum {w in WIDTHS} w * rolls[w,p];
1 63.84 3 59.41 5 64.09 7 62.82 9 59.66 # material used
2 61.75 4 61.24 6 62.54 8 62.0
                                              # in each pattern
ampl: display sum {p in PATTERNS}
ampl? Cut[p] * (rawWidth - sum {w in WIDTHS} w * rolls[w,p]);
62.32
                                              # total waste
                                              # in solution
ampl: display OrderLimits.lslack;
6.77 0
                                              # overruns
7.56 0
                                              # of each pattern
17.46 0
18.76 5
```

AMPL Script

Trade off two objectives

- ✤ Minimize rolls cut
 - * Fewer overruns, possibly more waste
- ✤ Minimize waste
 - * Less waste, possibly more overruns

```
minimize TotalCut:
    sum {p in PATTERNS} Cut[p];
minimize TotalWaste:
    sum {p in PATTERNS}
    Cut[p] * (rawWidth - sum {w in WIDTHS} w * rolls[w,p]);
```

AMPL Script

Parametric Analysis of Tradeoff

Minimize rolls cut

✤ Set large overrun limit in data

Minimize waste

- ✤ Reduce overrun limit 1 roll at a time
- ✤ If there is a change in number of rolls cut
 - record total waste (increasing)
 - * record total rolls cut (decreasing)
- Stop when no further progress possible
 - * problem becomes infeasible *or*
 - * total rolls cut falls to the minimum
- Report table of results

AMPL Script **Parametric Analysis** (cont'd)

```
Script (setup and initial solve)
```

```
model cutTradeoff.mod:
data cutTradeoff.dat;
set OVER default {} ordered by reversed Integers;
param minCut;
param minCutWaste;
param minWaste {OVER};
param minWasteCut {OVER};
param prev_cut default Infinity;
option solver gurobi;
option solver_msg 0;
objective TotalCut;
solve >Nul;
let minCut := TotalCut;
let minCutWaste := TotalWaste;
objective TotalWaste;
```

AMPL Script **Parametric Analysis** (cont'd)

Script (looping and reporting)

```
for \{k \text{ in overrun } \dots 0 \text{ by } -1\}
   let overrun := k;
   solve >Nul;
   if solve_result = 'infeasible' then break;
   if TotalCut < prev_cut then {
      let OVER := OVER union {k};
      let minWaste[k] := TotalWaste;
      let minWasteCut[k] := TotalCut;
      let prev_cut := TotalCut;
   ጉ
   if TotalCut = minCut then break;
}
printf 'Min%3d rolls with waste%6.2f\n\n', minCut, minCutWaste;
printf ' Over Waste Cut\n';
printf {k in OVER}: '%4d%8.2f%5d\n', k, minWaste[k], minWasteCut[k];
```

AMPL Script **Parametric Analysis** (cont'd)

04

Script run

<pre>ampl: include cutWASTE.run</pre>							
Min 20	rolls	with waste	62.				
Over	Waste	Number					
25	40.57	24					
19	43.01	23					
13	45.45	22					
7	47.89	21					
5	54.76	20					
ampl:							

Modeling Language APIs (Application Programming Interfaces)

Example: Roll Cutting by Pattern Enumeration

fill orders for rolls of various widths

Given

- Demands, raw width, orders, overrun limit at before
- ✤ pattern generation software
- ✤ result reporting software

Build optimization into an integrated application

- use AMPL for model-based optimization
- use a general-purpose programming language for overall control, pattern generation, and reporting

AMPL API AMPL API

Principles

- APIs for "all" popular languages
 C++, C#, Java, MATLAB, Python, R
- Common overall design
- ✤ Common implementation core in C++
- Customizations for each language and its data structures

Key to examples: Python and R

- ✤ AMPL entities
- AMPL API Python/R objects
- AMPL API Python/R methods
- Python/R functions etc.

AMPL API AMPL Model File

Same pattern-cutting model

```
param nPatterns integer > 0;
set PATTERNS = 1..nPatterns; # patterns
set WIDTHS; # finished widths
param order {WIDTHS} >= 0; # rolls of width j ordered
param overrun; # permitted overrun on any width
param rawWidth; # width of raw rolls to be cut
param rolls {WIDTHS,PATTERNS} >= 0, default 0;
# rolls of width i in pattern j
var Cut {PATTERNS} integer >= 0; # raw rolls to cut in each pattern
minimize TotalRawRolls: sum {p in PATTERNS} Cut[p];
subject to FinishedRollLimits {w in WIDTHS}:
    order[w] <= sum {p in PATTERNS} rolls[w,p] * Cut[p] <= order[w] + overrun;</pre>
```

AMPL API Some Python Data

A float, an integer, and a dictionary

```
roll_width = 64.5
overrun = 6
Orders = {
    6.77: 10,
    7.56: 40,
    17.46: 33,
    18.76: 10
}
```

... can also work with lists and Pandas dataframes

AMPL API Some R Data

A float, an integer, and a dataframe

```
roll_width <- 64.5
overrun <- 6
orders <- data.frame(
   width = c( 6.77, 7.56, 17.46, 18.76 ),
   demand = c( 10, 40, 33, 10 )
)</pre>
```

Load & generate data, set up AMPL model

```
def cuttingEnum(dataset):
    from amplpy import AMPL

    # Read orders, roll_width, overrun
    exec(open(dataset+'.py').read(), globals())

    # Enumerate patterns
    widths = list(sorted(orders.keys(), reverse=True))
    patmat = patternEnum(roll_width, widths)

    # Set up model
    ampl = AMPL()
    ampl.option['ampl_include'] = 'models'
    ampl.read('cut.mod')
```

Load & generate data, set up AMPL model

```
cuttingEnum <- function(dataset) {
    library(rAMPL)

    # Read orders, roll_width, overrun
    source(paste(dataset, ".R", sep=""))

    # Enumerate patterns
    patmat <- patternEnum(roll_width, orders$width)
    cat(sprintf("\n%d patterns enumerated\n\n", ncol(patmat)))

    # Set up model
    ampl <- new(AMPL)
    ampl$setOption("ampl_include", "models")
    ampl$read("cut.mod")
</pre>
```

Send data to AMPL

```
# Send scalar values
ampl.param['nPatterns'] = len(patmat)
ampl.param['overrun'] = overrun
ampl.param['rawWidth'] = roll_width
# Send order vector
ampl.set['WIDTHS'] = widths
ampl.param['order'] = orders
# Send pattern matrix
ampl.param['rolls'] = {
  (widths[i], 1+p): patmat[p][i]
  for i in range(len(widths))
   for p in range(len(patmat))
}
```

Send data to AMPL

```
# Send scalar values
```

```
ampl$getParameter("nPatterns")$set(ncol(patmat))
ampl$getParameter("overrun")$set(overrun)
ampl$getParameter("rawWidth")$set(roll_width)
```

```
# Send order vector
```

```
ampl$getSet("WIDTHS")$setValues(orders$width)
ampl$getParameter("order")$setValues(orders$demand)
```

```
# Send pattern matrix
```

```
df <- as.data.frame(as.table(patmat))
df[,1] <- orders$width[df[,1]]
df[,2] <- as.numeric(df[,2])</pre>
```

```
ampl$getParameter("rolls")$setValues(df)
```

Solve and get results

```
# Solve
ampl.option['solver'] = 'gurobi'
ampl.solve()
# Retrieve solution
CuttingPlan = ampl.var['Cut'].getValues()
cutvec = list(CuttingPlan.getColumn('Cut.val'))
```

Solve and get results

```
# Solve
ampl$setOption("solver", "gurobi")
ampl$solve()
# Retrieve solution
CuttingPlan <- ampl$getVariable("Cut")$getValues()
solution <- CuttingPlan[CuttingPlan[,-1] != 0,]</pre>
```

Display solution

```
# Prepare solution data
summary = \{
    'Data': dataset,
    'Obj': int(ampl.obj['TotalRawRolls'].value()),
    'Waste': ampl.getValue(
                 'sum {p in PATTERNS} Cut[p] * \
                     (rawWidth - sum {w in WIDTHS} w*rolls[w,p])'
             )
}
solution = [
    (patmat[p], cutvec[p])
    for p in range(len(patmat))
    if cutvec[p] > 0
٦
# Create plot of solution
cuttingPlot(roll_width, widths, summary, solution)
```

Display solution

```
# Prepare solution data
data <- dataset
obj <- ampl$getObjective("TotalRawRolls")$value()
waste <- ampl$getValue(
    "sum {p in PATTERNS} Cut[p] * (rawWidth - sum {w in WIDTHS} w*rolls[w,p])"
)
summary <- list(data=dataset, obj=obj, waste=waste)
# Create plot of solution
cuttingPlot(roll_width, orders$width, patmat, summary, solution)
}
```

Enumeration routine

```
def patternEnum(roll_width, widths, prefix=[]):
    from math import floor
    max_rep = int(floor(roll_width/widths[0]))
    if len(widths) == 1:
        patmat = [prefix+[max_rep]]
    else:
        patmat = []
        for n in reversed(range(max_rep+1)):
            patmat += patternEnum(roll_width-n*widths[0], widths[1:], prefix+[n])
        return patmat
```

Enumeration routine

```
patternEnum <- function(roll_width, widths, prefix=c()) {</pre>
  cur_width <- widths[length(prefix)+1]</pre>
  max_rep <- floor(roll_width/cur_width)</pre>
  if (length(prefix)+1 == length(widths)) {
      return (c(prefix, max_rep))
  } else {
      patterns <- matrix(nrow=length(widths), ncol=0)</pre>
      for (n in 0:max_rep) {
          patterns <- cbind(</pre>
               patterns,
               patternEnum(roll_width-n*cur_width, widths, c(prefix, n))
      return (patterns)
  }
}
```

Plotting routine

```
def cuttingPlot(roll_width, widths, summ, solution):
    import numpy as np
    import matplotlib.pyplot as plt
    ind = np.arange(len(solution))
    acc = [0]*len(solution)
    colorlist = ['red','lightblue','orange','lightgreen',
                          'brown','fuchsia','silver','goldenrod']
```

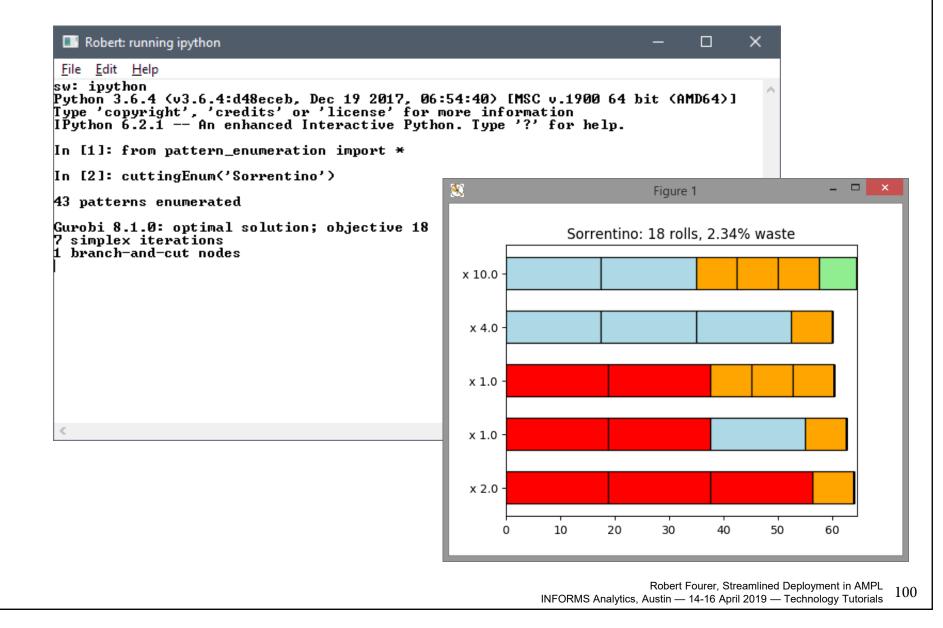
Plotting routine

```
cuttingPlot <- function(roll_width, widths, patmat, summary, solution) {
  pal <- rainbow(length(widths))
  par(mar=c(1,1,1,1))
  par(mfrow=c(1,nrow(solution)))
  for(i in 1:nrow(solution)) {
    pattern <- patmat[, solution[i, 1]]
    data <- c()
    color <- c()}</pre>
```

Plotting routine (cont'd)

```
for p, (patt, rep) in enumerate(solution):
   for i in range(len(widths)):
      for j in range(patt[i]):
         vec = [0]*len(solution)
         vec[p] = widths[i]
         plt.barh(ind, vec, 0.6, acc,
                   color=colorlist[i%len(colorlist)], edgecolor='black')
         acc[p] += widths[i]
plt.title(summ['Data'] + ": " +
   str(summ['Obj']) + " rolls" + ", " +
   str(round(100*summ['Waste']/(roll_width*summ['Obj']),2)) + "% waste"
plt.xlim(0, roll_width)
plt.xticks(np.arange(0, roll_width, 10))
plt.yticks(ind, tuple("x {:}".format(rep) for patt, rep in solution))
plt.show()
```

Plotting routine (cont'd)



🖙 RGui (64-bit)					– 🗆 X		
File History Resize Windows							
R Console				23			
<pre>> source("PatternEnumeration.R") > cuttingEnum("Sorrentino")</pre>	R Graphics: Dev						
95 patterns enumerated	x 3	x 5	x 1	x 8	x 1		
\$data							
[1] "Sorrentino"							
\$obj [1] 18							
\$waste							
[1] 27.12							
>							
<							

Modeling Language Integration with Python and Jupyter Notebooks

Example: Roll Cutting by Pattern Generation

- Sending Python data to an AMPL model
 - * via AMPL API for Python
 - * via Python references in the AMPL model
- Programming a custom stopping criterion in Python
 * via callbacks from the Gurobi solver
- Maintaining a view of the integrated application
 * via Jupyter notebooks

Example: Lot Sizing using Advanced Formulations

- Generating specialized constraints
 - * via Python embedded in AMPL scripts

Python Integration

Sending Python Data to an AMPL model

Imported and generated data in Python

```
roll_width = 64.5
overrun = 6
orders = {
    6.77: 10,
    7.56: 40,
    17.46: 33,
    18.76: 10
}
patmat = patternEnum(ro)
```

patmat = patternEnum(roll_width, list(sorted(orders.keys(), reverse=True)))

Python Integration Sending Data using the Python API

Symbolic sets and parameters in AMPL

```
param nPatterns integer > 0;
set PATTERNS = 1..nPatterns;
set WIDTHS;
param order {WIDTHS} >= 0;
param overrun;
param rawWidth;
param rolls {WIDTHS,PATTERNS} >= 0, default 0;
```

cut.mod

Python Integration Sending Data using the Python API (cont'd)

Call amp1 methods to read model, send data

```
ampl = AMPL()
.....
ampl.param['nPatterns'] = len(patmat)
ampl.param['overrun'] = overrun
ampl.param['rawWidth'] = roll_width
ampl.set['WIDTHS'] = widths
ampl.param['order'] = orders
ampl.param['rolls'] = {
   (widths[i], 1+p): patmat[p][i]
   for i in range(len(widths))
   for p in range(len(patmat))
}
```

Python Integration Sending Data using PyMPL

Specify Python data correspondences in the model

```
ampl = AMPL(langext=PyMPL())
.....
$PARAM[nPatterns]{ len(patmat) };
set PATTERNS = 1..nPatterns;
$SET[WIDTHS]{ widths };
$PARAM[order{^WIDTHS}]{ orders };
$PARAM[order{^WIDTHS}]{ orders };
$PARAM[overrun]{ overrun };
$PARAM[rawWidth]{ roll_width };
$PARAM[rolls {^WIDTHS,^PATTERNS}]{
    {
        (widths[i], 1+p): patmat[p][i]
        for i in range(len(widths))
        for p in range(len(patmat))
    }
};
```

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cutpy.mod

Callbacks

Example: User-specified stopping rule

Data

- ♦ Times $t_1 < t_2 < t_3$ etc.
- ✤ Optimality gap tolerances $g_1 < g_2 < g_3$ etc.

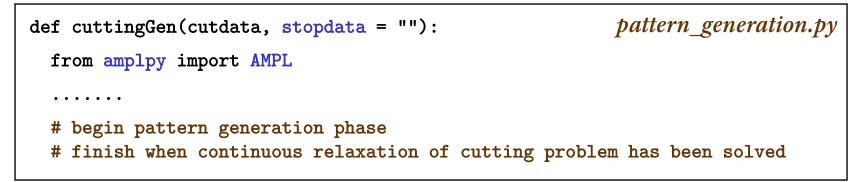
Execution

- * When elapsed time reaches $t_i \dots$
- ✤ Increase the gap tolerance to g_i

Python Integration Callbacks

Stopping rule data in Python dictionary

Main routine for cutting by pattern generation



stopping.py

Python Integration Callbacks

Set up callback and solve final integer program

```
# Instead of Master.solve(), export to a gurobipy object
grb_model = Master.exportGurobiModel()
# Assign AMPL stopping data to gurobipy objects
if len(stopdata) == 0:
  grb_model._stoprule = {'time': (1e+10,), 'gaptol': (1,)}
else:
  exec(open(stopdata+'.py').read(), globals())
  stopdict['time'] += (1e+10,)
  stopdict['gaptol'] += (1,)
  grb_model._stoprule = stopdict
grb_model._current = 0
# Solve and import results
grb_model.optimize(callback)
Master.importGurobiSolution(grb_model)
```

Python Integration Callbacks

Callback function

```
def callback(m, where):
    """Gurobi callback function."""
    if where == gpy.GRB.Callback.MIP:
        runtime = m.cbGet(gpy.GRB.Callback.RUNTIME)
        if runtime >= m._stoprule['time'][m._current]:
            print("Reducing gap tolerance to %f at %d seconds" % \
               (m._stoprule['gaptol'][m._current], m._stoprule['time'][m._current]))
        m.Params.MIPGap = m._stoprule['gaptol'][m._current]
        m._current += 1
```

Fix AMPL variables according to Python variable

Invoke Python generators for special lot-sizing constraints

\$EXEC{

```
def mrange(a, b):
    return range(a, b+1)
s = ['s[{}]'.format(t) for t in mrange(0, NT)]
y = ['y[{}]'.format(t) for t in mrange(1, NT)]
d = [demand[t] for t in mrange(1, NT)]
if BACKLOG is False:
    WW_U_AMPL(s, y, d, NT, prefix='w')
else:
    r = ['r[{}]'.format(t) for t in mrange(1, NT)]
    WW_U_B_AMPL(s, r, y, d, NT, prefix='w')
};
```

```
ampl = AMPL(langext=PyMPL())
ampl.read('lotsize.mod')
ampl.solve()
```

lotsize.mod

Optional listing of generated constraints

```
var ws {wi in 0..8} = s[wi];
var wr {wi in 1..8} = r[wi];
var wy {wi in 1..8} = y[wi];
param wD {1...8, 1...8};
data:
param wD :=
[1,1]400 [1,2]800 [1,3]1600 [1,4]2400 [1,5]3600 [1,6]4800 [1,7]6000 [1,8]7200
[2,1]0 [2,2]400 [2,3]1200 [2,4]2000 [2,5]3200 [2,6]4400 [2,7]5600 [2,8]6800
[3,1]0
      [3,2]0 [3,3]800 [3,4]1600 [3,5]2800 [3,6]4000 [3,7]5200 [3,8]6400
[4,1]0
      [4,2]0 [4,3]0 [4,4]800 [4,5]2000 [4,6]3200 [4,7]4400 [4,8]5600
[5,1]0
      [5,2]0 [5,3]0 [5,4]0 [5,5]1200 [5,6]2400 [5,7]3600 [5,8]4800
[6.1]0
      [6,2]0 [6,3]0 [6,4]0 [6,5]0 [6,6]1200 [6,7]2400 [6,8]3600
[7,1]0
      [7,2]0 [7,3]0 [7,4]0 [7,5]0 [7,6]0 [7,7]1200 [7,8]2400
                        [8,4]0 [8,5]0 [8,6]0 [8,7]0
[8,1]0
       [8,2]0 [8,3]0
                                                              [8,8]1200
;
model;
```

Optional listing of generated constraints (cont'd)

```
var wa {1..8};
var wb {1..8};
subject to wXY {wt in 1..8}: wa[wt] + wb[wt] + wy[wt] >= 1;
subject to wXA {wk in 1..8, wt in wk..min(8, wk+8-1): wD[wt,wt]>0}:
    ws[wk-1] >=
        sum {wi in wk..wt} wD[wi,wi] * wa[wi]
        - sum {wi in wk..wt-1} wD[wi+1,wt] * wy[wi];
subject to wXB {wk in 1..8, wt in max(1, wk-8+1)..wk: wD[wt,wt]>0}:
    wr[wk] >=
        sum {wi in wt..wk} wD[wi,wi] * wb[wi]
        - sum {wi in wt..wk} wD[wi,wi] * wb[wi]
        - sum {wi in wt..wk} wD[wi,wi] * wb[wi];
```

AMPL in Jupyter Notebooks

Mix AMPL and Python cells

🔜 F 🧼 L 💋 C 🛎 #	🔽 T 🕬 V 🐲 S 🛛 F 🗙 C 🚰 (🛐 C 🦻 V 🛤 C 🗢 F	
\leftrightarrow \rightarrow C (i) localhos	t:8888/notebooks/pattern_generation2.ipynb#Imports	5 📜 🏘
💭 jupyt	er pattern_generation2 (unsaved changes)	Cogout
File Edit	t View Insert Cell Kernel Widgets Help	Trusted Python 3 O
	Code ▼	
	AMPLPY: Pattern Generation	
	Documentation: <u>http://amplpy.readthedocs.io</u>	
	GitHub Repository: <u>https://github.com/ampl/amplpy</u>	
	PyPI Repository: <u>https://pypi.python.org/pypi/amplpy</u>	
	PyPI Repository: <u>https://pypi.python.org/pypi/amplpy</u>	
	PyPI Repository: <u>https://pypi.python.org/pypi/amplpy</u>	
In [1	<pre>Imports]: fromfuture import print_function</pre>	
In [1	Imports	

Building a Decision-Making Tool for Deployment

QuanDec

- ✤ Implemented in the Java API for AMPL
- Developed and supported by Cassotis Consulting

QuanDec Architecture

Server side

- AMPL model and data
- Standard AMPL-solver installations

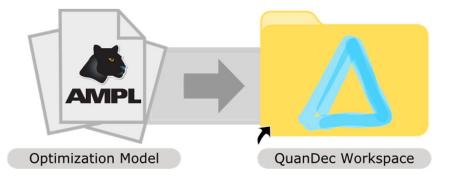
Client side

- Interactive tool for collaboration & decision-making
- Runs on any recent web browser
- ✤ Java-based implementation
 - * AMPL API for Java
 - * Eclipse Remote Application Platform

QuanDec Getting Started

step 1: install QuanDec on a server

- step 2: copy & paste your model files (.mod and .dat) into QuanDec's workspace
- step 3: create AMPL tables and link them to QuanDec explorer



QuanDec Workbench

Workspace	Admin			QuanAec
Explorer		Viewer	Report tables	Input tables
section 1 section 2 category 2.1 category 2.2 category 2.3		Charts Wate Barle Hops Yeas	Export	 Import Edit values Edit set: new/remove/ duplicate Comment
		Journal Bounds Reg	ressions Comments	Console >_

QuanDec Scenarios

	non, moe	differences	🍇 Expo					-		an		
omparator					10	Economics and Production	×				0	
ariable	Unit	BUDGET 2016	Ay Scenario	Diff		Variable	Index	Unit	BUDGET 2016 M	y Scenario	Pier	1
Executive summaries					-	Economics per int. plant	'PLT' 'costs'	MUS\$	1515.59	1515.20	-0.0:	Scenario
S Costs and Revenues						Economics per int. plant	'PLT' 'revenues'	MUS\$	1762.23	1761.77	-0.0:	Scenario
Profit and Sales						Economics per int. plant	'PLT' 'profit'	MUS\$	246.64	246.56		comparison
🛛 飾 Production costs						Economics per int. plant	'PLT' 'margin'	%	14.00	14.00		
Absolute costs	MUS\$					Production cost of product	'PLT' 'coke'	US\$/t	164.48	164.54		
> Detailed costs	US\$/t					Production cost of product	'PLT' 'sinter'	US\$/t	77.55		-0.06%	
Internal price of interm	edia US\$/t					Production cost of product	'PLT' 'hotmetal'	US\$/t	193.95	193.99		1
A Net production level	kt				=	Production cost of product	'PLT' 'slab'	US\$/t	286.27	286.28	10000	All variables can
'PLT' 'CO'	kt	1763.98	1764.25	0.02%		Production cost of product	'PLT' 'electricity'	US\$/MW		125.75	CONCERNMENT OF THE OWNER OF THE O	All valiables call
'PLT' 'SI'	kt	4085.77	4084.46	-0.03%		Production level of product	'PLT' 'coke'	kt	1818.54	1818.81	1000	be compared
'PLT' 'BF'	kt	5062.62	5060.91			Production level of product	PLI Sinter	kt	4085.77	4084.46	-0.0.	be compared
'PLT' 'ST'	kt	5258.29	5256.75			Report Structure						
'PLT' 'PO'												
		the scenarios to	o compare:			Reports					125	1
Production cost of production	> _ {	BUDGET 20:	15			Name	User		Date		Acti	Display of relative
Production level	-	BUDGET 20	16			Sulfur cycle	Benjami	n Steward	March 18, 2016 3:4	45 PM	×	Display of relative
Material blends		My Scena	ario			Metallic blend at CV	Me		February 21, 2016	4:51 PM	×	difference
Coke plants		FORECAST 2		_		Raw material use at Reducti	on Me		January 15, 2016 4	1:36 PM	×	
Sinter plants	- ° 🗆 (- TORECHOT I	LUIT			Economics and Production	Mary To	тes	September 13, 201	6 4:53 PM	×	1
Blast furnaces						Flux consumption at Torped	Mary To	res	April 3, 2016 4:44	PM	×	1
Steel shops						Slab sales	Robert F	inn	January 30, 2016 5	5:30 PM	×	
🕨 🦻 Power plant				- 1		Silicon cycle	Benjami		July 5, 2016 4:17 I		×	Custom reports
👞 Raw materials					Ŧ	Sincorregele	benjami	i otenuru	July 5, 2010 4.17 1	14	~	custom reports