# Adding Optimization to Your Applications *Quickly and Reliably*

1. A Guide to Model-Based Optimization 2. From Prototyping to Integration with AMPL

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INFORMS Business Analytics Conference Technology Workshop, 3 April 2022

> Adding Optimization to Your Applications, Quickly and Reliably INFORMS Business Analytics Conference — 3 April 2022

# Outline

### 1. Model-based optimization

### 2. From prototyping to integration

- Suilding models: AMPL's interactive environment
- Developing optimization-based procedures: AMPL scripts
- Integrating into decision-making systems: AMPL APIs

### 3. Case studies

- \* assignment: Dropbox
- \* packing: Young's Plant Farm
- \* deployment: ABB / Hitachi Energy

# **Example:** Roll Cutting

### Motivation

- ✤ Fill orders for rolls of various widths
  - \* by cutting raw rolls of one (large) fixed width
  - \* using a variety of cutting patterns

### **Optimization model**

- Decision variables
  - \* number of raw rolls to cut according to each pattern
- Objective

\* minimize number of raw rolls used

- Constraints
  - \* meet demands for each ordered width

# Roll Cutting Mathematical Formulation

## Given

- W set of ordered widths
- *n* number of patterns considered

## and

- $a_{ij}$  occurrences of width *i* in pattern *j*, for each  $i \in W$  and j = 1, ..., n
- $b_i$  orders for width i, for each  $i \in W$

4

### Roll Cutting Mathematical Formulation (cont'd)

### Determine

 $\begin{array}{ll} X_j & \text{number of rolls to cut using pattern } j, \\ & \text{for each } j = 1, \dots, n \end{array}$ 

to minimize

 $\sum_{j=1}^{n} X_{j}$ 

total number of rolls cut

subject to

 $\sum_{j=1}^{n} a_{ij} X_j \ge b_i$ , for all  $i \in W$ 

number of rolls cut of width *i* must be at least the number ordered

# Roll Cutting AMPL Formulation

#### Symbolic model

```
set WIDTHS;
param orders {WIDTHS} > 0;
param nPAT integer >= 0;
param nbr {WIDTHS,1..nPAT} integer >= 0;
var Cut {1..nPAT} integer >= 0;
minimize Number:
   sum {j in 1..nPAT} Cut[j];
subj to Fulfill {i in WIDTHS}:
   sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

```
\sum_{j=1}^{n} a_{ij} X_j \ge b_i, for all i \in W
```

6

# Roll Cutting **AMPL Formulation** (cont'd)

Explicit data (independent of model)

```
param: WIDTHS: orders :=
6.77 10
7.56 40
17.46 33
18.76 10 ;
param nPAT := 9 ;
param nbr: 1 2 3 4 5 6 7 8 9 :=
6.77 0 1 1 0 3 2 0 1 4
7.56 1 0 2 1 1 4 6 5 2
17.46 0 1 0 2 1 0 1 1 1
18.76 3 2 2 1 1 1 0 0 0 ;
```

# **Command Environment**

*Model* + *data* = *problem instance to be solved* 

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver cplex;
ampl: solve;
CPLEX 20.1.0.0: optimal integer solution; objective 20
3 MIP simplex iterations
0 branch-and-bound nodes
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13 7 4 9 3
```

# **Command Language** (cont'd)

Solver choice independent of model and data

```
ampl: model cut.mod;
ampl: data cut.dat;
ampl: option solver gurobi;
ampl: solve;
Gurobi 9.5.1: optimal solution; objective 20
3 simplex iterations
1 branch-and-cut nodes
ampl: option omit_zero_rows 1;
ampl: option display_1col 0;
ampl: display Cut;
4 13 7 4 9 3
```

# **Command Language** (cont'd)

### Results available for browsing

| <pre>ampl: display {j in 1nPAT} sum {i in WIDTHS} i * nbr[i,j];</pre>  |                            |  |  |
|--|----------------------------|--|--|
| 1 63.84 3 59.41 5 64.09 7 62.82 9 59.66 #  | <pre># material used</pre> |  |  |
| 2 61.75 4 61.24 6 62.54 8 62.03 <b>#</b>   | f in each pattern          |  |  |
| <pre>ampl: display {j in 1nPAT, i in WIDTHS: Cut[j] &gt; 0]</pre>  | <pre>hbr[i,j];</pre>       |  |  |
| : 4 7 9 := #   | <pre># patterns used</pre> |  |  |
| 6.77 0 0 4   |                            |  |  |
| 7.56 1 6 2   |                            |  |  |
| 17.46 2 1 1  |                            |  |  |
| 18.76 1 0 0  |                            |  |  |
| <pre>ampl: display Fulfill.slack; 6.77 2 ### Comparison of Comparison ## Comparison of Comparison ## Comparison of Comparison ## Comparison of Comparison ## Comparison of Comparison of</pre> | t overruns                 |  |  |
| 7.56 3   | f of each width            |  |  |
| 17.46 0  |                            |  |  |
| 18.76 3  |                            |  |  |

# Roll Cutting Revision 1

### Symbolic model

```
param roll_width > 0;
set WIDTHS;
param orders {WIDTHS} > 0;
param nPAT integer >= 0;
param nbr {WIDTHS,1..nPAT} integer >= 0;
var Cut {1..nPAT} integer >= 0;
minimize Number:
   sum {j in 1...nPAT} Cut[j];
minimize Waste:
   sum {j in 1...nPAT}
      Cut[j] * (roll_width - sum {i in WIDTHS} i * nbr[i,j]);
subj to Fulfill {i in WIDTHS}:
   sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

### Roll Cutting Revision 1 (cont'd)

#### Explicit data

```
param roll_width := 64.5;
param: WIDTHS: orders :=
       6.77
              10
       7.56
              40
      17.46
            33
      18.76
            10;
param nPAT := 9 ;
param nbr:
         1 2 3 4 5 6 7 8 9 :=
         0 1 1 0 3 2 0 1 4
    6.77
    7.56 1 0 2 1 1 4 6 5 2
   17.46 0 1 0 2 1 0 1 1 1
   18.76
          3 2 2
                1
                    1
                     1
                         0 0
                             0;
```

# **Revision 1** (cont'd)

#### **Solutions**

```
ampl: model cutRev1.mod;
ampl: data cutRev1.dat;
ampl: objective Number; solve;
Gurobi 9.5.1: optimal solution; objective 20
3 simplex iterations
1 branch-and-cut nodes
ampl: display Number, Waste;
Number = 20
Waste = 63.62
ampl: objective Waste; solve;
Gurobi 9.5.1: optimal solution; objective 15.62
2 simplex iterations
1 branch-and-cut nodes
ampl: display Number, Waste;
Number = 35
Waste = 15.62
```

# Roll Cutting Revision 2

### Symbolic model

### Roll Cutting Revision 2 (cont'd)

#### Explicit data

```
param roll_width := 64.5;
param over_lim := 8 ;
param: WIDTHS: orders :=
       6.77
              10
       7.56
            40
      17.46 33
      18.76 10;
param nPAT := 9 ;
param nbr:
          1 2 3 4 5 6 7 8 9 :=
          0 1 1 0 3 2 0 1 4
    6.77
    7.56 1 0 2 1 1 4 6 5 2
   17.46 0 1 0 2 1 0 1 1 1
   18.76
          3 2 2 1
                     1 0 0
                    1
                              0;
```

# **Revision 2** (cont'd)

#### **Solutions**

```
ampl: model cutRev2.mod;
ampl: data cutRev2.dat;
ampl: objective Number; solve;
Gurobi 9.5.1: optimal solution; objective 20
7 simplex iterations
1 branch-and-cut nodes
ampl: display Number, Waste;
Number = 20
Waste = 62.04
ampl: objective Waste; solve;
Gurobi 9.5.1: optimal solution; objective 40.57
5 simplex iterations
1 branch-and-cut nodes
ampl: display Number, Waste;
Number = 24
Waste = 40.57
```

# Scripting

## Bring the programmer to the modeling language

## Extend existing modeling language syntax . . .

- Algebraic expressions
- Set indexing expressions
- Interactive commands

## ... with programming concepts

- ✤ Loops of various kinds
- ✤ If-then and If-then-else conditionals
- Assignments

## Examples

- Tradeoffs between *number cut* and *waste*
- Cutting via pattern enumeration
- Cutting via pattern generation

#### Scripting

# **Tradeoffs Between Objectives**

#### Minimize rolls cut

✤ Set large overrun limit

#### Minimize waste

- ✤ Reduce overrun limit 1 roll at a time
- ✤ If there is a change in number of rolls cut
  - record total waste (increasing)
  - \* record total rolls cut (decreasing)
- Stop when no further progress possible
  - \* problem becomes infeasible
  - \* total rolls cut falls to the minimum
- Report table of results

# Scripting **Parametric Analysis** (cont'd)

```
Script (setup and initial solve)
```

```
model cutRev2.mod;
data cutRev2.dat;
set OVER default {} ordered by reversed Integers;
param minNumber;
param minNumWaste;
param minWaste {OVER};
param minWasteNum {OVER};
param prev_number default Infinity;
option solver gurobi;
option solver_msg 0;
objective Number;
solve >Nul;
let minNumber := Number;
let minNumWaste := Waste;
objective Waste;
```

# Scripting **Parametric Analysis** (cont'd)

Script (looping and reporting)

```
for \{k \text{ in over}_{lim} \dots 0 \text{ by } -1\}
   let over_lim := k;
   solve >Nul;
   if solve_result = 'infeasible' then break;
   if Number < prev_number then {</pre>
      let OVER := OVER union {k};
      let minWaste[k] := Waste;
      let minWasteNum[k] := Number;
      let prev_number := Number;
   ጉ
   if Number = minNumber then break;
}
printf 'Min%3d rolls with waste%6.2f\n\n', minNumber, minNumWaste;
printf ' Over Waste Number\n';
printf {k in OVER}: '%4d%8.2f%6d\n', k, minWaste[k], minWasteNum[k];
```

# Scripting Parametric Analysis (cont'd)

04

#### Script run

| <pre>ampl: include cutWASTE.run</pre> |       |            |     |  |
|---------------------------------------|-------|------------|-----|--|
| Min 20                                | rolls | with waste | 62. |  |
| Over                                  | Waste | Number     |     |  |
| 25                                    | 40.57 | 24         |     |  |
| 19                                    | 43.01 | 23         |     |  |
| 13                                    | 45.45 | 22         |     |  |
| 7                                     | 47.89 | 21         |     |  |
| 5                                     | 54.76 | 20         |     |  |
| ampl:                                 |       |            |     |  |

#### Scripting

# Cutting via Pattern Enumeration

### Build the pattern list, then solve

- ✤ Read general model
- ✤ Read data: demands, raw width
- ✤ Compute data: all usable patterns
- ✤ Solve problem instance

### Model

```
param roll_width > 0;
set WIDTHS ordered by reversed Reals;
param orders {WIDTHS} > 0;
param maxPAT integer >= 0;
param nPAT integer >= 0, <= maxPAT;
param nbr {WIDTHS,1..maxPAT} integer >= 0;
var Cut {1..nPAT} integer >= 0;
minimize Number:
   sum {j in 1..nPAT} Cut[j];
subj to Fulfill {i in WIDTHS}:
   sum {j in 1..nPAT} nbr[i,j] * Cut[j] >= orders[i];
```

#### Data

### Script (initialize)

```
model cutPAT.mod;
param dsetname symbolic;
printf "\nEnter dataset name:\n";
read dsetname <-;</pre>
data (dsetname & ".dat");
model;
param curr_sum >= -1e-10;
param curr_width > 0;
param pattern {WIDTHS} integer >= 0;
let maxPAT := 10000000;
let nPAT := 0;
let curr_sum := 0;
let curr_width := first(WIDTHS);
let {w in WIDTHS} pattern[w] := 0;
```

## Script (loop)

```
repeat {
   if curr_sum + curr_width <= roll_width then {
      let pattern[curr_width] := floor((roll_width-curr_sum)/curr_width);
      let curr_sum := curr_sum + pattern[curr_width] * curr_width;
   if curr_width != last(WIDTHS) then
      let curr_width := next(curr_width,WIDTHS);
   else {
      let nPAT := nPAT + 1;
      let {w in WIDTHS} nbr[w,nPAT] := pattern[w];
      let curr_sum := curr_sum - pattern[last(WIDTHS)] * last(WIDTHS);
      let pattern[last(WIDTHS)] := 0;
      let curr_width := min {w in WIDTHS: pattern[w] > 0} w;
      if curr_width < Infinity then {
         let curr_sum := curr_sum - curr_width;
         let pattern[curr_width] := pattern[curr_width] - 1;
         let curr_width := next(curr_width,WIDTHS);
      else break;
   }
```

Script (solve, report)

```
printf "\nAT LEAST %d ROLLS REQUIRED\n\n",
    ceil((sum {i in WIDTHS} i * orders[i]) / roll_width);
option solver gurobi;
solve;
printf "\n%5i patterns, %3i rolls", nPAT, sum {j in 1..nPAT} Cut[j];
printf "\n\n Cut ";
printf {j in 1..nPAT: Cut[j] > 0}: "%3i", Cut[j];
printf "\n\n";
for {i in WIDTHS} {
    printf "%7.2f ", i;
    printf {j in 1..nPAT: Cut[j] > 0}: "%3i", nbr[i,j];
    printf "\n";
    }
```

#### Results

```
ampl: include cutPatEnum.run
AT LEAST 18 ROLLS REQUIRED
Gurobi 9.5.1: optimal solution; objective 18
4 simplex iterations
1 branch-and-cut nodes
43 patterns, 18 rolls
Cut 2 1 1 4 10
18.76 3 2 2 0 0
17.46 0 1 0 3 2
7.56 1 1 3 1 3
6.77 0 0 0 0 1
```

#### Data 2

param roll\_width := 349 ; param: WIDTHS: orders := 28.75 7 33.75 23 34.75 23 31 37.75 38.75 10 39.75 39 40.75 58 41.75 47 42.25 19 13 44.75 26; 45.75

#### Results 2

ampl: include cutPatEnum.run AT LEAST 34 ROLLS REQUIRED Gurobi 9.5.1: optimal solution; objective 34 126 simplex iterations 1 branch-and-cut nodes 54508 patterns, 34 rolls Cut 8 1 1 5 1 2 2 5 2 1 1 4 1 45.75 3 1 0 0 0 0 0 0 0 0 0 0 0 44.75 1 3 0 0 0 0 0 0 0 0 0 0 0 4 6 4 1 0 0 0 42.25 0 0 0 0 0 41.75 4 0 0 0 1 6 2 0 0 0 0 0 0 40.75 0 0 0 2 0 1 1 6 5 5 3 0 0 0 0 0 0 0 0 2 0 1 0 4 4 2 39.75 0 2 0 1 0 0 0 1 0 0 0 0 38.75 0 0 2 0 1 0 0 4 1 0 0 1 0 37.75 0 34.75 0 0 0 0 0 0 2 3 0 0 0 0 0 33.75 0 0 0 0 7 0 0 0 2 2 2 0 6 1 2 2 2 0 28.75 0 0 0 0 0 0 0 1

#### Data 3

param roll\_width := 172 ; param: WIDTHS: orders := 25.000 5 24.750 73 18.000 14 17.500 4 23 15.500 15.375 5 13.875 29 12.500 87 12.250 9 31 12.000 10.250 6 10.125 14 10.000 43 8.750 15 8.500 21 5; 7.750

Results 3 (using 1% of generated patterns)

```
ampl: include cutPatEnum.run
AT LEAST 33 ROLLS REQUIRED
Gurobi 9.5.1: optimal solution; objective 33
493 simplex iterations
1 branch-and-cut nodes
273380 patterns, 33 rolls
  Cut
             5 5 5
                       1 1 1 4 6 2 1 1 1
  25.00
             1 0 0 0 0 0 0 0 0 0 0 0

      24.75
      1
      5
      3
      2
      2
      2
      2
      1
      0
      0
      0

      18.00
      0
      1
      0
      2
      2
      0
      0
      1
      3
      0
      0

  17.50 0 0 0 0 0 4 0 0 0 0 0 0
   . . . . . . .
  10.12
             0 0 2 0 0
                                0 0 0
                                            0 2 2 0
             0 \quad 0 \quad 0 \quad 0 \quad 2 \quad 0 \quad 0 \quad 6 \quad 0 \quad 4 \quad 1 \quad 0
  10.00
   8.75 1 0 0 1 0 0 2 0 1 1 0 2
             2 0 0 0 5 0 0 3 0 0 0
   8.50
                               0 0 0
                                            0
    7.75
             0 1
                    0 0
                            0
                                                0 0
                                                        0
```

# Scripting in practice . . .

## Large and complex scripts

- ✤ Multiple files
- Hundreds of statements
- Millions of statements executed

## Coordination with enterprise systems

- ✤ Your system
  - \* writes data files
  - \* invokes ampl optapp.run
- ✤ AMPL's script
  - \* reads the data files
  - \* processes data, generates problems, invokes solvers
  - \* writes result files
- ✤ Your system
  - **\*** reads the result files

# Scripting Limitations

### Scripts can be slow

- Interpreted, not compiled
- Very general set & data structures

### Script programming constructs are limited

- ✤ Based on a declarative language
- Not object-oriented

### Scripts are stand-alone

- ✤ Run in a separate AMPL environment
- Challenging to package, integrate, and deploy

# **APIs** (application programming interfaces)

## Bring the modeling language to the programmer

- Data and result management in a general-purpose programming language
- Modeling and solving through calls to AMPL

## Available in all AMPL distributions

\* **Python** 2.7, 3.*x* 

\* pip install amplpy

### ✤ C++, C#, MATLAB, Java

\* Download from https://ampl.com/products/api/

#### \* R

- \* install.packages("Rcpp", type="source")
- \* install.packages(

"https://ampl.com/dl/API/rAMPL.tar.gz", repos=NULL)

# AMPL API Cutting Revisited

## Hybrid approach

- Control & pattern enumeration from a programming language
- Model definition & modeling commands in AMPL

## Key to examples: Python and R

- ✤ AMPL entities
- AMPL API Python/R objects
- AMPL API Python/R methods
- Python/R functions etc.
Load & generate data, set up AMPL model

```
def cuttingEnum(dataset):
    from amplpy import AMPL

    # Read orders, roll_width, overrun
    exec(open(dataset+'.py').read(), globals())

    # Enumerate patterns
    widths = list(sorted(orders.keys(), reverse=True))
    patmat = patternEnum(roll_width, widths)

    # Set up model
    ampl = AMPL()
    ampl.option['ampl_include'] = 'models'
    ampl.read('cut.mod')
```

#### Send data to AMPL

```
# Send scalar values
ampl.param['nPatterns'] = len(patmat)
ampl.param['overrun'] = overrun
ampl.param['rawWidth'] = roll_width
# Send order vector
ampl.set['WIDTHS'] = widths
ampl.param['order'] = orders
# Send pattern matrix
ampl.param['rolls'] = {
  (widths[i], 1+p): patmat[p][i]
  for i in range(len(widths))
   for p in range(len(patmat))
}
```

#### Solve and get results

```
# Solve
ampl.option['solver'] = 'gurobi'
ampl.solve()
# Retrieve solution
CuttingPlan = ampl.var['Cut'].getValues()
cutvec = list(CuttingPlan.getColumn('Cut.val'))
```

#### Display solution

```
# Prepare solution data
summary = \{
    'Data': dataset,
    'Obj': int(ampl.obj['TotalRawRolls'].value()),
    'Waste': ampl.getValue(
                 'sum {p in PATTERNS} Cut[p] * \
                     (rawWidth - sum {w in WIDTHS} w*rolls[w,p])'
             )
}
solution = [
    (patmat[p], cutvec[p])
    for p in range(len(patmat))
    if cutvec[p] > 0
٦
# Create plot of solution
cuttingPlot(roll_width, widths, summary, solution)
```

#### **Enumeration routine**

```
def patternEnum(roll_width, widths, prefix=[]):
    from math import floor
    max_rep = int(floor(roll_width/widths[0]))
    if len(widths) == 1:
        patmat = [prefix+[max_rep]]
    else:
        patmat = []
        for n in reversed(range(max_rep+1)):
            patmat += patternEnum(roll_width-n*widths[0], widths[1:], prefix+[n])
        return patmat
```

#### **Plotting routine**

*Plotting routine (cont'd)* 

```
for p, (patt, rep) in enumerate(solution):
   for i in range(len(widths)):
      for j in range(patt[i]):
         vec = [0]*len(solution)
         vec[p] = widths[i]
         plt.barh(ind, vec, 0.6, acc,
                   color=colorlist[i%len(colorlist)], edgecolor='black')
         acc[p] += widths[i]
plt.title(summ['Data'] + ": " +
   str(summ['Obj']) + " rolls" + ", " +
   str(round(100*summ['Waste']/(roll_width*summ['Obj']),2)) + "% waste"
plt.xlim(0, roll_width)
plt.xticks(np.arange(0, roll_width, 10))
plt.yticks(ind, tuple("x {:}".format(rep) for patt, rep in solution))
plt.show()
```



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#### AMPLAPI APIs in practice . . .

#### Application system in chosen programming language

- Extract requirements from enterprise database
- ✤ Generate good patterns to consider
- ✤ Feed results to visualization and deployment systems

#### Key role for modeling in AMPL

- Prototype and refine a model
- ✤ Evolve and maintain the model reliably
- Manage the interface to chosen solvers

### *Case:* Dropbox *Sales Representative Assignment*



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### Application

#### Setting

- Cloud storage provider
- ✤ Over 500 million users upload 1.2 billion files every day
- Tens of thousands of large business customer accounts
- Hundreds of sales representatives worldwide
  - \* enough to cover most but not all accounts

#### Goal

- ✤ Assign accounts to representatives
  - \* Assign each representative a similar number and quality of accounts
  - \* Give priority to assigning higher quality accounts

#### Sales Rep Assignment Evaluation

#### Approaches considered

- ✤ Manual system
- Spreadsheet-based solvers
- Automated system using model-based optimization

#### Choice of AMPL

- ✤ Ease of use
- \* Speed
- ✤ Reliability
- ✤ Ability to handle large problems

#### Sales Rep Assignment Formulation (data and variables)

#### Data

- Quality *score* for each customer account
  - \* predicted revenue increase if contacted by a representative
- Location of each representative

#### Decision variables

For each account *i* and representative *j*,
 *X<sub>ij</sub>* = 1 if account *i* is assigned to representative *j X<sub>ij</sub>* = 0 otherwise

#### Sales Rep Assignment **Formulation** (objective and constraints)

#### **Objective**

Maximize total score of all assigned accounts

#### Constraints

- ✤ At most 15% variance between representatives in . . .
  - \* number of accounts assigned
  - \* quality of accounts assigned
- ✤ Assigned accounts must be near the representative's location
- ✤ All subaccounts of a business must have the same representative

## Sales Rep Assignment Implementation

#### Development

Implementation by 3 analysts at Dropbox

#### **Optimization**

- Mixed-integer linear solver
- ✤ 10,000 zero-one variables
- ✤ 3-6 hours to solve for largest region

#### Deployment

- ✤ 5-10 sales leaders are direct users
- AMPL is embedded in Dropbox's systems
  - \* Customer data is extracted from *Salesforce*
  - \* Customer scores are computed using the *scikit-learn* Python toolbox
  - \* An AMPL script reads the file of score data
  - \* Results from optimization are written to an *Excel* spreadsheet

# *Case:* Young's Plant Farm *Packing and Shipping*



## Packing Application

#### Setting

- ✤ Grows plants of many kinds and sizes
- Ships to retailers on their own trucks
  \* Large customers include Walmart, Lowe's
- ✤ Plants are packed on special rolling racks
  - \* 3 feet wide, 4 feet long, 7 feet tall
  - **\*** 4 to 12 shelves



#### Goal

- ✤ Generate good packing plans for a day's orders
  - Don't use more racks than needed
- ✤ Finish in time to get the orders out

## Packing Evaluation

#### Approaches considered

- Spreadsheet "by hand"
- ✤ Algebraic modeling language + integer linear solver

#### Choice of AMPL

- Dramatically better solutions
- Numerous economies
  - ✤ Faster solutions using many fewer people
  - ✤ Faster loading of racks
  - ✤ Fewer trucks required
- Selection of solvers

## Packing **Formulation**

#### Data

- Set of stores
- Numbers of each plant ordered by each store
- Number of packing patterns: Ways that a rack may be packed
  - ✤ Up to several million, generated each day
- Number of each plant in each packing pattern
  - ✤ Up to six different plants per rack

#### Variables: all 0 or 1

- ✤ Whether a pattern is used at all
- ✤ Whether a store uses a certain pattern
- Whether a plant is shipped to a certain store using a certain pattern

## Packing **Formulation**

#### **Objective:** Minimize

- ✤ Racks used, plus penalties . . .
  - ✤ for not using all space in a pattern
  - ✤ for using all space in a tightly packed pattern

#### **Constraints**

- For each type of plant, the number of plants shipped to a store must equal the number of plants ordered by the store
- If a pattern is not used at all, then it cannot be used for any store
- If a pattern is not used for a particular store, then it cannot be used to send the store any of the plants it contains

#### Packing Implementation

#### Development

- ✤ Original model built by Prof. Rafay Ishfaq of Auburn University
- Extended to handle larger orders by AMPL Optimization

#### **Optimization**

- Implemented using AMPL model, data, and scripts
- Minimum size: low 100s of thousands of variables & constraints Maximum size: 100 *million* variables & constraints
- Solve time: 10 to 45 minutes

#### Deployment

- VBA-modified spreadsheet for data prep and result reporting
- One replenishment specialist uses the tool multiple times a day

... considering adaptations to new use cases

### Case: ABB Managing Power Grids



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77

### Case: ABB Power Grid Management

### GridView

For studies within the Western Electric Coordinating Council territory, GridView provides an industry-accepted simulation approach. The advanced analysis methodology combines generation, transmission, loads, fuels, and market economics into one integrated framework to

deliver location dependent market indicators, transmission system utilization measures and power system reliability and market performance indices. It provides invaluable information for both generation and transmission planning, operational decision making and risk management.

GridView uses state-of-the-art modeling technology to simulate security-constrained unit commitment and economic dispatch. It produces unit commitment and economic dispatch that respect the physical laws of power flow and transmission reliability requirements. As such, the generation dispatch and market clearing price are feasible market solutions within real power transmission networks.

## Power Grid Application

#### Setting

- Power grid operators provide electrical service
- Two kinds of decisions
  - \* *Unit commitment:* When to turn power plants on and off
  - \* *Network flow:* How to transmit power over the grid to meet demand

#### Goal

- Simulate optimal decisions to support planning
  - \* Transmission network expansion
  - \* Plant addition and retirement
  - \* Integration of renewable energy sources

### Power Grid Evaluation

#### Approaches considered

- ✤ C++ for entire GridView system
- Modeling language for optimization, C++ for user interfaces

#### Choice of AMPL

- ✤ Ease of modeling
  - \* ABB can formulate complex and powerful models
  - \* Customers can understand the AMPL formulations
  - \* Customers can specialize models to their particular situations
- ✤ Ease of embedding
  - \* Optimization can be built into the GridView product using AMPL's C++ API

#### Power Formulation (data)

#### **Production data**

- Power generation units
  - \* Location
  - \* Fuel, design, age, capacity
  - \* Ramp-up and ramp-down times
- ✤ Renewable energy sources

#### Transmission network data

- Nodes: units, sources, substations, customers
  - \* Supply at plants and other sources
  - \* Demand at customers
- ✤ Arcs: power lines
  - \* Transmission capacities

#### Cost data

#### Power Formulation (variables)

#### Decision variables

- $\boldsymbol{\ast}\,$  For each unit, in each time period
  - \* On or off (discrete)
  - \* Level of output (continuous)
- \* For each *critical path* through the grid, in each time period
  - \* Capacity

#### Power Formulation (model)

#### **Objectives**

- For short-term operation management
  - \* Minimize total operating costs
- For long-term investment planning
  - \* Minimize total operating and investment costs

#### **Constraints**

- ✤ Balance of supply and demand
- Capacity restriction on power lines
- Ramp-up and ramp-down times
- Contingencies for generation and transmission

## Power Grid Implementation

#### Development

- ✤ Prototype at University of Tennessee, Knoxville
- ✤ Full AMPL implementation by three analysts at ABB

#### **Optimization**

- Mixed-integer linear solver
- Millions of variables
- Tens of thousands of integer variables
- ✤ 10 minutes to solve

#### Deployment

- ✤ 30+ customer companies
- Hundreds of customer-side users

### Case: Hitachi Energy Managing Power Grids

Simulate security-constrained unit commitment and economic dispatch in largescale transmission networks



Adding Optimization to Your Applications, Quickly and Reliably INFORMS Business Analytics Conference — 3 April 2022

85

### *Case:* Hitachi Energy *Managing Distributed Power Grids*

Digital solutions for distributed energy resources



Infinite insight

e-mesh

**@Hitachi Energy** 

### *Case:* Hitachi Energy *Distributed Power Grid Management*

### e-mesh<sup>™</sup>: Infinite insight

The e-mesh<sup>™</sup> digital ecosystem enables the digitalization of distributed energy resources.

The power generation infrastructure is decentralized, consumers are becoming prosumers, and the aging grid system is unable to accommodate this new transition. In parallel, renewables are also steadily increasing, and with the emergence of IoT, cloud and low-cost battery energy storage systems, the power system has become highly complex today. While this trend is contributing to sustainable energy production, it also helps to provide energy independence for participating stakeholders such as commercial and industrial enterprises, independent power producers, and remote communities. The challenge remaining for all stakeholders is how to adapt to this new decentralized model.

Hitachi Energy e-mesh<sup>™</sup> helps global customers to easily transition to this new distributed energy model. From the field to the boardroom, we enable our customers to accelerate performance and stay ahead of the curve.

## Distributed Power Application

#### Setting

- ✤ Power grids are changing radically
  - \* The infrastructure is decentralizing
  - \* Small-scale renewable sources are being added
  - \* Low-cost battery storage systems are becoming available
  - \* Consumers are becoming power generators, too
- ✤ The current grid system is challenged to adapt

#### Goal

- Build a new product for distributed power planning
- Extend the ABB GridView optimization tools to management of renewables and batteries

### Distributed Power Evaluation

#### Only approach considered

 Extend GridView's AMPL models to handle complications posed by new technologies

#### Choice of AMPL

- ✤ Existing features
  - \* Speed, familiarity
  - \* Mature APIs
- Licensing for new deployment formats, such as *containers*

## Distributed Power Sample Formulation

#### Overview

- Network-constrained unit commitment problem
- ✤ Mix of renewable sources & battery storage, within a microgrid

#### **Decision variables**

- ✤ Binary: Whether a plant / battery is on or off at a given time
- \* *Continuous:* Bi-directional power flows over transmission links

#### Objective

- ✤ Minimize total costs . . .
  - \* Generation
  - \* Transmission
  - \* Supplemental (externally sourced) power
- ✤ ... summed over a given time horizon

#### Distributed Power Sample Formulation (cont'd)

#### **Objective**

- Minimize total costs
  - **\*** Generation
  - \* Transmission
  - \* Supplemental (externally sourced) power
- summed over a given time horizon

#### **Constraints**

- Transmission link capacity
- ✤ Battery charge and discharge rates
- ✤ Battery capacity
- Demand satisfaction
# Distributed Power Implementation

#### Project

- Created at ABB Italy (now part of Hitachi Energy)
- ✤ 6 project members interacted with AMPL

## Tools

- ✤ AMPL Python API
- ✤ VS Code editor for collaboration
- Docker containers, Kubernetes container management
- Amazon Web Services
- D3.js for visualization

## **Optimization**

- Mixed-integer linear solver
- ✤ 200K to 45M variables and constraints
- ✤ 30 seconds to 20 minutes for each run

# Distributed Power Deployment

#### Current (2022)

- Testing with 5-10 commercial clients
- Expect 30+ adoptions within 2 years

## **Ongoing benefits**

- Optimization is essential to grid management
- ✤ AMPL enables the core commercial utility of e-mesh

### Future possibilities

- Expand e-mesh's portfolio of features
- Support vehicle charging and electric fleet optimization

# *Technology Tutorial:* Optimization in Your Toolchain: How AMPL is Making it Faster and Easier

Tuesday, 9:10-10:00 am

Room Sugarland A

- Expressing constraint logic more directly and understandably
- Exchanging data and results directly and efficiently with spreadsheets and database systems
- Interfacing to business systems through APIs for popular programming languages
- Deploying optimization in cloud environments and containers